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Research Article

Prefiltering-Based Interference Suppression for Time-Hopping Multiuser UWB Communications over MISO Channel

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This paper proposes a prefiltering-based scheme for pulsed ultra-wideband (UWB) system by shifting the signal processing needs from the receiver at the radio terminal (RT) to the transmitter at the fixed access point (AP) where power and computational resources are plentiful. We exploit antenna array in the transmitter of AP and take advantage of the spatial and temporal diversities to mitigate the multiuser interference (MUI) as well as preequalize the channel impulse response (CIR) of a time-hopping (TH) multiple access UWB communication system. Three prefiltering schemes are developed to meet different criteria. A simple correlation receiver is proposed at the RT to combine the desired signal stemmed from all the transmitting antennas. The performances under different scenarios are extensively evaluated over multiple-input single-output (MISO) channels.

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1. Introduction

Recently, a lot of attention was paid to UWB impulse radio systems since it is a promising technique for low-complexity low-power short-range indoor wireless communications [1–5]. When such transmissions are applied in multiple access system, time-hopping (TH) spreading codes are a plausible choice to separate different users [6–8]. Modulation of TH impulse radio is accomplished by assigning user-specific pattern of time shifting of pulses.

The time-reversal- (TR-) based UWB scheme has been extensively investigated recently [9–13]. Attractive features of TR signal processing include the following.

- (1) It makes full use of the energy from all the resolvable paths: it can create space and time focalization at a specific point where signals are coherently added [9, 12].
- (2) Channel estimation in UWB system is generally a difficult task. Most UWB networks have APs, and the TR-based UWB technique shifts the sophisticated channel estimation burden from the receivers of radio terminal (RT) to the AP. This is also referred to as the "prerake" diversity combining scheme [14].

(3) Quite a few data-aided and blind timing acquisition schemes have been proposed [15–18] for UWB transmission through dense multipath channels. Synchronization in TR UWB scheme is extremely simplified since the peak is automatically created and aligned of the received signal at specific time slot.

Most past works of TR UWB scheme focus on the issue of single-user transmission and detection. The topic of multiuser TR UWB scheme has been analyzed in [19]. With different approach, we employ TH codes and address the applicability of zero-forcing (ZF) and least squares (LS) techniques to further improve system performance. The communication system considered in this paper consists of M transmitting antennas at the AP, K single-antenna RT, which indicates K individual MISO channels. Signal separation is accomplished by

- (1) user-specific TH codes that are designed as "orthogonal" as possible, that is, locate each user's pulse train in nonoverlapping time slots.
- (2) user-specific CIR that is determined by each user's spatial location.

In this paper, we propose three prefiltering schemes, where a set of M prefilters are designated to each user

at the transmitter of the AP. The prefilters of the first scheme are derived to meet the ZF criterion such that MUI is completely removed at the receiver front end of RT. Thereby, a simple single-user correlator can be employed at RT receiver to maximize output signal-to-noise ratio (SNR). When the degrees of freedom are insufficient for complete MUI suppression, an LS-based scheme is also proposed to mitigate MUI. The third scheme is composed of a set of TR matchedfilters (MFs) at the transmitter that correlate to the MISO CIR. Since the TR MF technique with application in the MISO UWB system has excellent spatial-temporal focusing capability, the energy of the received signal tends to concentrate on some controllable time slots. This enables us to implement a simple correlation receiver to extract the energy at these time slots where peak occur.

The remainder of this paper is organized as follows. In Section 2, we formulate the signal and channel models of the time-hopping UWB multiple access communication system over frequency-selective fading channel. Section 3 highlights the rationale of the prefiltering-based multiuser UWB MISO system, where three prefiltering schemes are proposed for signal transmission and detection. Simulation results are presented and analyzed in Section 4. Concluding remarks are finally made in Section 5.

Notation. The boldface letters represent vector or matrix. $\mathbf{A}(i,j)$ denotes the element of ith row and jth column of matrix \mathbf{A} , $\mathbf{x}(l)$ denotes the lth element of vector \mathbf{x} , and $[]^T$ and $[]^H$ stand for transpose and complex transpose of a matrix or vector, respectively. We will use $E\{\}$ for expectation (ensemble average), $\|\cdot\|$ for vector norm, and := for "is defined as." Also, "*" indicates the linear convolution operation, \mathbf{I}_M denotes an identity matrix with size M, and $\mathbf{0}_M$, $\mathbf{1}_M$ are $M \times 1$ vectors with all elements being 0 and 1, respectively. Finally, $\delta(\cdot)$ is the dirac delta function.

2. Signal and Channel Models

2.1. Signal Model. In UWB impulse radios, every information symbol (bit) is conveyed by N_f data modulated ultrashort pulses over N_f frames. There is only one pulse in each frame, and the frame duration is T_f . The pulse waveform, p(t), is referred to as a monocycle [1] with ultrashort duration T_c at the nanosecond scale. The energy of p(t) is normalized within T_c to unity, so that $\int_0^{T_c} |p(t)|^2 dt = 1$. Note that T_f is usually a hundred to a thousand times of chip duration, T_c , which accounts for very low duty cycle. When multiple users are simultaneously transmitted and received, signal separation can be accomplished with user-specific pseudorandom TH codes, which shift the pulse position in every frame. The binary (antipodal) PAM scheme is considered, thus we may establish the signal model designated for the kth RT as

$$s_{k}(t) = \sum_{i} a_{k} d_{k}(i) c_{k}(t)$$

$$= \sum_{i} a_{k} d_{k}(i) \sum_{j=0}^{N_{f}-1} p(t - iN_{f}T_{f} - jT_{f} - c_{j}^{k}T_{c}),$$
(1)

where t is the clock time of the transmitter, and i is the bit index. a_k is the amplitude. Binary information bit $d_k(i)$ takes on the value ± 1 with equal probability. $c_k(t) :=$ $\sum_{j=0}^{N_f-1} p(t-iN_fT_f-jT_f-c_j^kT_c)$ represents the specific waveform assigned for the kth RT. Denoting T_b as the bit duration, then $T_b = N_f T_f$. Suppose each frame is composed of N_c time slots each with duration T_c , thus, $T_f = N_c T_c$. User separation is accomplished by user-specific pseudo-random TH code. $\{c_j^k\}_{j=0,\dots,N_f-1}$ accounts for the kth user's TH code with period N_f . Thereby $c_j^k T_c$ is the time-shift of the pulse position imposed by the TH sequence employed for multiple access. $c_i^k T_c \leq T_f$, or equivalently, $0 \leq c_i^k \leq N_c - 1$. Note that to avoid the presence of intersymbol interference (ISI), we let the last frame for each user being empty (without pulse). This is equivalent to adding a guard time T_f at the end of each bit. Specifically, T_f , which is up to our disposal, should be longer than the sum of delay spread (maximum dispersion), T_d , of the CIR and the prefilter length. Based on the signal model of (1), the transmitted bit energy for the kth user can be calculated as $E_{b,k} = (N_f - 1)a_k^2$. $E_{b,k}$ is chosen to meet the FCC regulated power level such that the UWB technology is allowed to overlay already available services.

2.2. Channel Model. Most of the envisioned commercial UWB applications will be indoor communications. The CIR as observed in the measurement of indoor environment can be expressed in general as [20]

$$h(t) = \sum_{n=0}^{N} \sum_{l=0}^{L} \alpha_{n,l} \exp(j\phi_{n,l}) \delta(t - T_n - \tau_{n,l}),$$
 (2)

where $\alpha_{n,l}$ and $\phi_{n,l}$ are the gain (attenuation) and phase of the 1th multipath component (MPC) of the 1th cluster, respectively. $T_n + \tau_{n,l} (\tau_{n,0} = 0)$ denotes the arrival time of the lth MPC of the nth cluster. Cluster arrivals and the subsequent arrivals within each cluster are modeled as Possion distribution with different rates. As described in [20], for some environments, most notably the industrial (CM9) and indoor office (CM4), "dense" arrivals of MPC were observed, that is, each resolvable delay bin contains significant energy. In these cases, the concept of ray arrival rates loses its meaning, and a realization of the impulse response- (IR-) based on a tapped delay line model with regular tap spacings is to be used, that is, a single cluster (N = 1), so that $\tau_{1,l} = \tau_l = l\Delta \tau$, where $\Delta \tau = T_c$ is the spacing of the delay taps. Moreover, the phase term, $\phi_{n,l}$, is also constrained to take values 0 or π with equal probability to account for the random pulse inversion due to reflection [21], so that $\exp(j\phi_{n,l}) = \pm 1$ with equal probability. This yields a real-valued channel model. Considering the above factors, the CIR of (2) can be reformulated as

$$h(t) = \sum_{l=0}^{L} \alpha_l \delta(t - lT_c), \tag{3}$$

where we model the multipath channel as a tapped-delay line with (L + 1) taps. α_l denotes the tap weight of the lth resolvable path. Note that in writing (3), we have implicitly

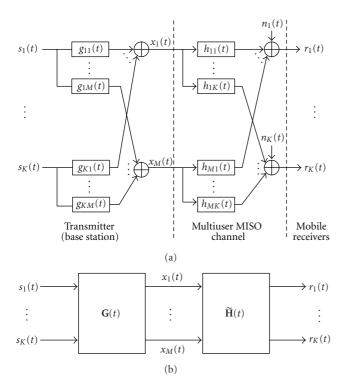


FIGURE 1: Schematic block diagram of a prefiltering-based MISO UWB communication system.

assumed that maximum time dispersion is LT_c . The channel fading coefficient α_l can be modeled as [22]

$$\alpha_l = b_l \xi_l, \tag{4}$$

where $b_l = \exp(j\phi_{n,l})$ is equiprobable to take on the value ± 1 . $\xi_l = |\alpha_l|$ is the log-normal fading magnitude term. The average power of α_l is represented by $E\{|\alpha_l|^2\} = \Omega_0 \exp(-\rho l)$. Ω_0 is a scalar for normalizing the power contained in resolvable paths, and ρ is the power decay factor. To simplify the analysis, we assume that the channel parameters are quasistatic (slowly fading) such that they are essentially constant over observation interval.

3. Design of Transmitters and Receivers in Prefiltered UWB MISO System

3.1. General Prefiltered UWB MISO System. As shown in Figure 1 of the considered structure, there are M transmitting antennas equipped at the AP, and each RT has single antenna. Let $h_{mk}(t) = \sum_{l=0}^L \alpha_{mk,l} \delta(t-lT_c)$ denote the CIR between the mth transmitting antenna and the kth RT, where $\alpha_{mk,l}$ represents the fading coefficient of the lth path. In the proposed prefiltering scheme, a set of MK finite impulse response (FIR) prefilters with IRs $g_{km}(t) = \sum_{p=0}^{p-1} \beta_{km,p} \delta(t-pT_c)$ are inserted, respectively, between $s_k(t)$ and the mth transmitting antenna. All users

are synchronously transmitted from the AP to all the RTs. Thereby, the transmitted waveform at the *m*th antenna is

$$x_m(t) = \sum_{k=1}^K s_k(t) * g_{km}(t); \quad m = 1, \dots, M,$$
 (5)

where K is the number of RTs. Upon defining $\mathbf{x}(t) := [x_1(t) \ x_2(t) \ \cdots \ x_M(t)]^T, \mathbf{s}(t) := [s_1(t) \ s_2(t) \ \cdots \ s_K(t)]^T$ and the $K \times M$ prefiltering matrix

$$\mathbf{G}(t) := \begin{bmatrix} g_{11}(t) & g_{12}(t) & \cdots & g_{1M}(t) \\ g_{21}(t) & g_{22}(t) & \cdots & g_{2M}(t) \\ \vdots & \ddots & \ddots & \vdots \\ g_{K1}(t) & g_{K2}(t) & \cdots & g_{KM}(t) \end{bmatrix}.$$
(6)

We may reexpress (5) as a compact form:

$$\mathbf{x}(t) = \mathbf{G}^{T}(t) * \mathbf{s}(t). \tag{7}$$

The channel between the AP and arbitrary RT can be regarded as a MISO system. Hence, the received signal at the *k*th RT can be formulated as

$$r_{k}(t) = \sum_{m=1}^{M} x_{m}(t) * h_{mk}(t) + n_{k}(t)$$

$$= \sum_{m=1}^{M} \left(\sum_{j=1}^{K} s_{j}(t) * g_{jm}(t) \right) * h_{mk}(t)$$

$$+ n_{k}(t); \quad k = 1, \dots, K$$

$$= \sum_{j=1}^{K} s_{j}(t) * \sum_{m=1}^{M} \left(g_{jm}(t) * h_{mk}(t) \right) + n_{k}(t),$$
(8)

where $n_k(t)$ is assumed to be zero-mean AWGN noise process with variance σ^2 (assume independent of k for simplicity). Similarly, let $\mathbf{r}(t) := [r_1(t) \quad r_2(t) \quad \cdots \quad r_K(t)]^T$, $\mathbf{n}(t) := [n_1(t) \quad n_2(t) \quad \cdots \quad n_K(t)]^T$ and the $M \times K$ MISO multiuser channel matrix

$$\widetilde{\mathbf{H}}(t) := \begin{bmatrix} h_{11}(t) & h_{12}(t) & \cdots & h_{1K}(t) \\ h_{21}(t) & h_{22}(t) & \cdots & h_{2K}(t) \\ \vdots & \ddots & \ddots & \vdots \\ h_{M1}(t) & h_{M2}(t) & \cdots & h_{MK}(t) \end{bmatrix}. \tag{9}$$

We may reformulate (8) into a more convenient form:

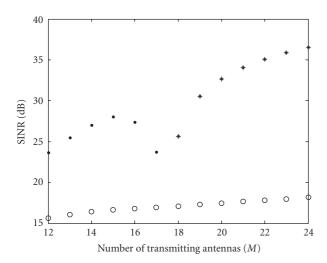
$$\mathbf{r}(t) = \widetilde{\mathbf{H}}^{T}(t) * \mathbf{x}(t) + \mathbf{n}(t)$$

$$= \widetilde{\mathbf{H}}^{T}(t) * \mathbf{G}^{T}(t) * \mathbf{s}(t) + \mathbf{n}(t)$$

$$= \left[\mathbf{G}(t) * \widetilde{\mathbf{H}}(t)\right]^{T} * \mathbf{s}(t) + \mathbf{n}(t)$$

$$= \mathbf{H}_{\text{eff}}^{T}(t) * \mathbf{s}(t) + \mathbf{n}(t),$$
(10)

where $\mathbf{H}_{\text{eff}}(t) := \mathbf{G}(t) * \widetilde{\mathbf{H}}(t)$ represents the "effective" FIR channel matrix with size $K \times K$.



- LS scheme
- * ZF scheme
- O TR-MF scheme

FIGURE 2: SINR performance with respect to the number of transmitting antennas.

3.2. Zero-Forcing- (ZF-) Based Scheme. To completely remove MUI, the MK prefilters should be designed to satisfy the following ZF criteria:

$$\sum_{m=1}^{M} \left(g_{jm}(t) * h_{mk}(t) \right)$$

$$= \begin{cases} 0, & j \neq k, \\ \eta_k \delta(t - LT_c), & j = k, \end{cases} \forall j, k = 1, \dots, K,$$

$$(11)$$

where LT_c is the delay introduced to accommodate the multipath effect. η_k accounts for the power normalization factor designated for each RT so that the transmitter bit energy remains constant independent of the number of transmit antennas. In other words, ZF-based prefilters attempt to design $\mathbf{G}(t)$ such that $\mathbf{H}_{\text{eff}}(t)$ reduces to a diagonal matrix

$$\mathbf{H}_{\text{eff}}^{(ZF)}(t) := \mathbf{G}^{(ZF)}(t) * \widetilde{\mathbf{H}}(t) = \begin{bmatrix} \eta_1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \eta_K \end{bmatrix} \delta(t - LT_c).$$
(12)

Denoting the discrete-time version $h_{mk}(t)$ as a (L+1) vector $\mathbf{h}_{mk} := [\alpha_{mk,0} \ \alpha_{mk,1} \ \cdots \ \alpha_{mk,L}]^T$, $g_{jm}(t) = \sum_{p=0}^{P-1} \beta_{jm,p} \ \delta(t-pT_c)$ as a P vector $\mathbf{g}_{jm} := [\beta_{jm,0} \ \beta_{jm,1} \ \cdots \ \beta_{jm,P-1}]^T$ (Here, we assume the order of

the FIR prefilters being P), respectively, then the discretetime counterparts of $g_{jm}(t) * h_{mk}(t)$ can be obtained as

$$\mathbf{H}_{mk}\mathbf{g}_{jm} = \begin{bmatrix} \alpha_{mk,0} & 0 & \cdots & \cdots & 0 \\ \vdots & \alpha_{mk,0} & \ddots & \ddots & \vdots \\ \alpha_{mk,L} & \vdots & \ddots & \ddots & \vdots \\ 0 & \alpha_{mk,L} & \ddots & \ddots & 0 \\ \vdots & 0 & \ddots & \ddots & \alpha_{mk,0} \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & \cdots & 0 & \alpha_{mk,L} \end{bmatrix} \begin{bmatrix} \beta_{jm,0} \\ \beta_{jm,1} \\ \vdots \\ \beta_{jm,P-1} \end{bmatrix},$$
(13)

where \mathbf{H}_{mk} is a $(L + P) \times P$ matrix as defined in (13). Using (13), we may convert (11) into

$$\mathbf{H}_{k}\mathbf{g}_{j} = \begin{cases} \mathbf{0}_{L+P}, & j \neq k, \\ \eta_{k}\mathbf{e}_{L}, & j = k, \end{cases}$$
(14)

where \mathbf{e}_L denotes the Lth column vector of $\mathbf{I}_{(L+P)}$. $\mathbf{H}_k := [\mathbf{H}_{1k} \ \mathbf{H}_{2k} \ \cdots \ \mathbf{H}_{Mk}]$ is a $(L+P) \times MP$ matrix, and $\mathbf{g}_j := [\mathbf{g}_{j1}^T \ \mathbf{g}_{j2}^T \ \cdots \ \mathbf{g}_{jM}^T]^T$ is a MP vector that incorporates the space-time IR of the jth user's prefilters. Upon defining the $K(L+P) \times MP$ matrix $\mathbf{H} := [\mathbf{H}_1^T \ \mathbf{H}_2^T \ \cdots \ \mathbf{H}_K^T]^T$ and the K(L+P) vector, $\mathbf{e}_L^{(k)} := [\mathbf{0}_{L+P}^T \ \cdots \ \mathbf{e}_L^T \ \cdots \ \mathbf{0}_{L+P}^T]^T$, we may reexpress (14) as

$$\mathbf{H}\mathbf{g}_k = \eta_k \mathbf{e}_L^{(k)},\tag{15}$$

where $\mathbf{e}_L^{(k)}$ denotes the (k(L+P)-P)th column vector of $\mathbf{I}_{K(L+P)}$.

If $K(L + P) \le MP$, which is up to our disposal (can be achieved by increasing M and/or P), we have infinitely many solutions since (15) is indeed an underdetermined system. The general solution includes a quiescent solution and a homogeneous solution that is chosen from the null (kernel) space of H:

$$\mathbf{g}_{k}^{(\mathrm{ZF})} = \eta_{k} \mathbf{H}^{T} (\mathbf{H} \mathbf{H}^{T})^{-1} \mathbf{e}_{L}^{(k)} + \mathbf{u}; \quad k = 1, \dots, K,$$
 (16)

where $\mathbf{H}\mathbf{u} = \mathbf{0}$. It should be noted that \mathbf{u} can be regarded as the surplus part of \mathbf{g}_k since it is useless for MUI suppression but only wastes transmission power. Thus, we let $\mathbf{u} = \mathbf{0}$ to minimize power consumption. Moreover, to guarantee the transmitted bit energy of the kth user to be $E_{b,k} = (N_f - 1)a_k^2$ independent of the prefilters and number of antennas, we choose η_k such that $\|\mathbf{g}_k\| = 1$. It follows from (16) (after removing \mathbf{u})

$$||\mathbf{g}_{k}||^{2} = \eta_{k}^{2} \mathbf{e}_{L}^{(k)}^{T} \left[\mathbf{H} \mathbf{H}^{T} \right]^{-1} \mathbf{e}_{L}^{(k)}$$

$$= \eta_{k}^{2} \left[\mathbf{H} \mathbf{H}^{T} \right]^{-1} (k(L+P) - P, k(L+P) - P)$$
(17)

Hence, η_k is chosen as

$$\eta_k^{(\mathrm{ZF})} = \frac{1}{\sqrt{[\mathbf{H}\mathbf{H}^T]^{-1}(k(L+P) - P, k(L+P) - P)}}.$$
 (18)

At the front end of each RT, chip-matched filtering (CMF) followed by chip-rate sampling, the discrete-time counterpart of $r_k(t)$, can be obtained as

$$r_k(n) = s_k(n) * \eta_k \delta(n - L) + n_k(n); \quad k = 1, ..., K,$$
 (19)

where the interference has been removed by ZF prefiltering. After bit-by-bit stacking, we arrive at a sequence of N_cN_f vectors. The samples of CMF output within the *i*th bit interval at the *k*th RT are

$$\mathbf{r}_k(i) = \eta_k a_k d_k(i) \mathbf{c}_{k,L} + \mathbf{n}_k(i), \tag{20}$$

where $\mathbf{c}_{k,L}$ stands for an L-chips delayed version of the kth user's TH code vector \mathbf{c}_k . The delay results from the criterion of (11). Since the MUI is completely removed, a simple correlation receiver can be employed that maximizes the averaged output SNR. The output signal (denoted as $z_k^{(ZF)}$), averaged SNR (denoted as $y_k^{(ZF)}$), and bit-error-rate (BER) (denoted as $Pe_k^{(ZF)}$) can be obtained in order:

$$z_{k}^{(ZF)}(i) = \mathbf{c}_{k,L}^{T} \mathbf{r}_{k}(i) = \eta_{k} a_{k} d_{k}(i) ||\mathbf{c}_{k,L}||^{2} + \mathbf{c}_{k,L}^{T} \mathbf{n}_{k}(i)$$

$$= \eta_{k} \left(N_{f} - 1 \right) a_{k} d_{k}(i) + \mathbf{c}_{k,L}^{T} \mathbf{n}_{k}(i),$$

$$y_{k}^{(ZF)} = \frac{\eta_{k}^{2} a_{k}^{2} \left(N_{f} - 1 \right)^{2}}{\sigma^{2} \left(N_{f} - 1 \right)} = \frac{\eta_{k}^{2} a_{k}^{2} \left(N_{f} - 1 \right)}{\sigma^{2}}, \qquad (21)$$

$$Pe_{k}^{(ZF)} = Q \left(\frac{\eta_{k} a_{k} \sqrt{\left(N_{f} - 1 \right)}}{\sigma} \right),$$

where $Q(x) := 1/\sqrt{2\pi} \int_{x}^{\infty} \exp(-(v^2/2)) dv$ is a monotonically decreasing function with respect to x.

If on the other hand, K(L+P) > MP, or equivalently K > MP/(L+P), the ZF criteria are inapplicable since there is insufficient degrees of freedom to suppress the interference. In other words, (15) becomes an overdetermined system. It is generally impossible to obtain exact solution. By minimizing the least-squares (minimum distance) criterion [23], we can obtain the kth user's prefilter as

$$\mathbf{g}_{k}^{(\mathrm{LS})} = \eta_{k} (\mathbf{H}^{T} \mathbf{H})^{-1} \mathbf{H}^{T} \mathbf{e}_{L}^{(k)}. \tag{22}$$

Similar to the derivation in (17) and (18), the power normalization factor can be obtained as

$$\eta_k^{(\mathrm{LS})} = \frac{1}{\sqrt{\left[\mathbf{H}(\mathbf{H}^T\mathbf{H})^{-2}\mathbf{H}^T\right](k(L+P) - P, k(L+P) - P)}},$$

$$k = 1, \dots, K.$$

Note that the LS solution can only "approximate" the ZF criteria. Therefore, the received signal at the *k*th RT should contain residual MUI:

$$\mathbf{r}_{k}(i) = \sum_{j=1}^{K} a_{j} d_{j}(i) \mathbf{c}_{j} * \mathbf{H}_{k} \mathbf{g}_{j} + \mathbf{n}_{k}(i)$$

$$= \sum_{j=1}^{K} \eta_{j} a_{j} d_{j}(i) \mathbf{c}_{jk} + \mathbf{n}_{k}(i),$$
(24)

where $\mathbf{c}_{jk} := \mathbf{c}_j * \mathbf{H}_k \mathbf{g}_j$. Applying the same correlator as ZF scheme, we can obtain the output averaged signal-to-interference-plus-noise ratio (SINR) as

$$\gamma_k^{(LS)} = \frac{\eta_k^2 a_k^2 \rho_k^2}{\sum_{j=1, j \neq k}^K a_j^2 \eta_j^2 \rho_j^2 + \sigma^2 (N_f - 1)},$$
 (25)

where $\rho_j := \mathbf{c}_{k,L}^T \mathbf{c}_{jk}$. With some manipulations, we can deduce the BER for the LS-based scheme:

 $PE_k^{(LS)}$

$$= 2^{1-K} \sum_{\substack{d_1 \cdots d_K \in \{-1,+1\} \\ d_k = 1}} Q \left(\frac{\eta_k a_k \rho_k + \sum_{j=1,j \neq k}^K \eta_j a_j \rho_j d_j}{\sigma_{\sqrt{N_f - 1}}} \right),$$

$$k = 1, \dots, K.$$
(26)

3.3. TR-MF-Based Scheme. In this scheme, a set of TR MFs with IRs $g_{km}(t) = \eta_{km}h_{mk}(T_d - t); k = 1, ..., K, m = 1, ..., M$ are placed at the transmitter as the prefilters, where T_d denotes the delay spread (maximum dispersion) of the CIR. In the considered model, $T_d = LT_c$, thus we may rewrite the IR of the TR MF as

$$g_{km}(t) = \eta_{km} h_{mk}(T_d - t) = \eta_{km} \sum_{l=0}^{L} \alpha_{mk, L-l} \delta(t - lT_c),$$

$$m = 1, \dots, M, \quad k = 1, \dots, K.$$
(27)

To guarantee that the energy per transmitted bit remains $E_{b,k} = (N_f - 1)a_k^2$ independent of the prefilters and number of antennas, it is easy to deduce that η_{km} should be chosen as

$$\eta_{km} = \frac{1}{\sqrt{M \sum_{l=0}^{L} \alpha_{mk,l-l}^2}} = \frac{1}{\sqrt{M} \|\mathbf{h}_{mk}\|}.$$
 (28)

Apparently, the order of the prefilters in the TR-MF scheme is the same as the MISO CIR. Let $\hat{h}_{mk}(T_d-t):=\eta_{km}h_{mk}(T_d-t)$, then the $K\times M$ prefiltering matrix for the TR MF scheme can be expressed as

$$\mathbf{G}^{(\mathrm{MF})}(t) := \begin{bmatrix} \hat{h}_{11}(T_d - t) & \hat{h}_{12}(T_d - t) & \cdots & \hat{h}_{1M}(T_d - t) \\ \hat{h}_{21}(T_d - t) & \hat{h}_{22}(T_d - t) & \cdots & \hat{h}_{2M}(T_d - t) \\ \vdots & \ddots & \ddots & \vdots \\ \hat{h}_{K1}(T_d - t) & \hat{h}_{K2}(T_d - t) & \cdots & \hat{h}_{KM}(T_d - t) \end{bmatrix}.$$
(29)

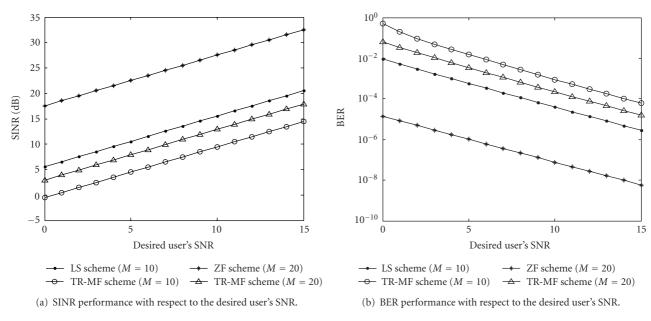


FIGURE 3: System performance with respect to the desired user's SNR.

The transmitted waveform at the *m*th antenna is

$$x_m(t) = \sum_{k=1}^K s_k(t) * \hat{h}_{mk}(T_d - t), \quad m = 1, \dots, M.$$
 (30)

Substituting (30) into (8), the received signal at the kth RT can be obtained as

$$r_{k}(t) = \sum_{m=1}^{M} x_{m}(t) * h_{mk}(t) + n_{k}(t)$$

$$= \sum_{m=1}^{M} \left\{ \sum_{j=1}^{K} s_{j}(t) * \hat{h}_{mj}(T_{d} - t) \right\} * h_{mk}(t) + n_{k}(t)$$

$$= \sum_{m=1}^{M} \left\{ s_{k}(t) * \hat{h}_{mk}(T_{d} - t) * h_{mk}(t) \right\}$$

$$+ \sum_{m=1}^{M} \sum_{\substack{j=1 \ j \neq k}}^{K} \left\{ s_{j}(t) * \hat{h}_{mj}(T_{d} - t) * h_{mk}(t) \right\} + n_{k}(t)$$

$$= \sum_{m=1}^{M} \left\{ s_{k}(t) * R_{mk}(t) \right\}$$

$$+ \sum_{m=1}^{M} \sum_{\substack{j=1 \ j \neq k}}^{K} \left\{ s_{j}(t) * R_{mj,mk}(t) \right\} + n_{k}(t)$$

$$= s_{k}(t) * R_{k}(t) + \sum_{\substack{j=1 \ j \neq k}}^{K} \left\{ s_{j}(t) * R_{j,k}(t) \right\} + n_{k}(t)$$

$$(31)$$

where $R_{mk}(t) := \hat{h}_{mk}(T_d - t) * h_{mk}(t)$ is the autocorrelation function of $h_{mk}(t)$, $R_{mj,mk}(t) := \hat{h}_{mj}(T_d - t) * h_{mk}(t)$ accounts

for the cross-correlation function between $h_{mk}(t)$ and $h_{mj}(t)$. $R_k(t) := \sum_{m=1}^M R_{mk}(t)$, $R_{j,k}(t) := \sum_{m=1}^M R_{mj,mk}(t)$. In what follows, the "effective" FIR channel matrix for the TR MF scheme yields

$$\mathbf{H}_{\text{eff}}^{(\text{MF})}(t) := \mathbf{G}^{(\text{MF})}(t) * \widetilde{\mathbf{H}}(t)$$

$$= \begin{bmatrix} R_{1}(t) & R_{1,2}(t) & \cdots & R_{1,K}(t) \\ R_{2,1}(t) & R_{2}(t) & \cdots & R_{2,K}(t) \\ \vdots & \vdots & \ddots & \vdots \\ R_{K,1}(t) & R_{K,2}(t) & \cdots & R_{K}(t) \end{bmatrix}$$
(32)

Denoting the discrete-time version of $h_{mk}(T_d - t) = \sum_{l=0}^{L} \alpha_{mk,L-l} \delta(t - lT_c)$ as an (L + 1) vector $\overline{\mathbf{h}}_{mk} := [\alpha_{mk,L} \cdots \alpha_{mk,1} \alpha_{mk,0}]^T$, then the discrete-time counterparts of $R_{mk}(t), R_{mj,mk}(t), R_k(t), R_{j,k}(t)$, respectively, can be formulated as

$$\mathbf{R}_{mk} = \eta_{km} \overline{\mathbf{h}}_{mk} * \mathbf{h}_{mk}$$

$$= \eta_{km} \begin{bmatrix} \alpha_{mk,L} & 0 & \cdots & \cdots & 0 \\ \vdots & \alpha_{mk,L} & \ddots & \ddots & \vdots \\ \alpha_{mk,0} & \vdots & \ddots & \ddots & \vdots \\ 0 & \alpha_{mk,0} & \ddots & \ddots & 0 \\ \vdots & 0 & \ddots & \ddots & \alpha_{mk,L} \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & \cdots & 0 & \alpha_{mk,0} \end{bmatrix} \mathbf{h}_{mk}$$
(33)

 $=\eta_{km}\overline{\mathbf{H}}_{mk}\mathbf{h}_{mk},$

$$\mathbf{R}_{mj,mk} = \eta_{jm} \overline{\mathbf{h}}_{mj} * \mathbf{h}_{mk} = \eta_{jm} \overline{\mathbf{H}}_{mj} \mathbf{h}_{mk}, \quad \forall j \neq k,$$

where $\overline{\mathbf{H}}_{mk}$, $\overline{\mathbf{H}}_{mj}$ are $(2L+1)\times(L+1)$ matrices. \mathbf{R}_{mk} , $\mathbf{R}_{mj,mk}$, \mathbf{R}_k , $\mathbf{R}_{j,k}$ all are vectors with size $(2L+1)\times 1$. Therefore, the magnitude of $\overline{\mathbf{h}}_{mk}*\mathbf{h}_{mk}$ will coherently add up at the central ((L+1)th) position of \mathbf{R}_{mk} , in which the magnitude of the peak is $\mathbf{R}_{mk}(L+1) = \eta_{km} \sum_{l=0}^{L} \alpha_{mk,l}^2 = \|\mathbf{h}_{mk}\|^2/\sqrt{M}\|\mathbf{h}_{mk}\| = \|\mathbf{h}_{mk}\|/\sqrt{M}$. On the other hand, the other terms of $\overline{\mathbf{h}}_{mj}*\mathbf{h}_{mk}$ will add up noncoherently and symmetrically distributed about $\mathbf{R}_{mk}(L+1)$:

$$\mathbf{R}_{k} = \sum_{m=1}^{M} \mathbf{R}_{mk} = \begin{bmatrix} \mathbf{R}_{1k} & \mathbf{R}_{2k} & \cdots & \mathbf{R}_{Mk} \end{bmatrix} \mathbf{1}_{M},$$

$$\mathbf{R}_{j,k} = \sum_{m=1}^{M} \mathbf{R}_{mj,mk} = \begin{bmatrix} \mathbf{R}_{1j,1k} & \mathbf{R}_{2j,2k} & \cdots & \mathbf{R}_{Mj,Mk} \end{bmatrix} \mathbf{1}_{M}.$$
(34)

It follows that the peak of $\mathbf{R}_k = \sum_{m=1}^M \mathbf{R}_{mk}$ is at $\mathbf{R}_k(L+1)$ with the magnitude further be enhanced as $\mathbf{R}_k(L+1) = 1/\sqrt{M} \sum_{m=1}^M \|\mathbf{h}_{mk}\|$.

The samples of CMF output within the *i*th bit interval at the *k*th RT can be expressed as

$$\mathbf{r}_{k}(i) = a_{k}d_{k}(i)\widetilde{\mathbf{c}}_{k} + \sum_{\substack{j=1\\j\neq k}}^{K} a_{j}d_{j}(i)\widetilde{\mathbf{c}}_{jk} + \mathbf{n}_{k}(i), \quad k = 1,\dots,K,$$
(35)

where \tilde{c}_k represents the effective signature vector of the kth user. It arises from the CMF output's chip-rate samples within a bit of the composite waveform, $c_k(t) * R_k(t)$. It is evident that \tilde{c}_k can be formulated as

$$\widetilde{\mathbf{c}}_k = \begin{bmatrix} \mathbf{c}_k & \mathbf{c}_{k,1} & \cdots & \mathbf{c}_{k,2L} \end{bmatrix} \mathbf{R}_k = \mathbf{C}_k \mathbf{R}_k,$$
 (36)

where each $\mathbf{c}_{k,l}$ stands for an l-chips delayed version of the kth user's TH code. \mathbf{C}_k is an $N_f N_c \times (2L+1)$ matrix. Similarly, we may formulate the jth $(j \neq k)$ user's effective signature vector at the kth RT as

$$\widetilde{\mathbf{c}}_{jk} = \begin{bmatrix} \mathbf{c}_j & \mathbf{c}_{j,1} & \cdots & \mathbf{c}_{j,2L} \end{bmatrix} \mathbf{R}_{j,k} = \mathbf{C}_j \mathbf{R}_{j,k}.$$
 (37)

Since the peak of \mathbf{R}_k is at $\mathbf{R}_k(L+1)$, thereby, after convolving with $c_k(t)$, this will shift the positions of the desired user's TH pulse train in $c_k(t)$ by (L+1) chips. Therefore, to capture the energy of the desired user, we propose to design a simple correlation receiver to extract the energies at the positions of these peak components. Therefore, the weight vector of the proposed correlation receiver should be chosen as $\mathbf{c}_{k,L}$. The output of the correlation receiver can be obtained as

$$z_k^{(MF)}(i) = \mathbf{c}_{k,L}^T \mathbf{r}_k(i)$$

$$= \mathbf{R}_k(L+1) \Big(N_f - 1 \Big) a_k d_k(i)$$

$$+ \mathbf{c}_{k,L}^T \sum_{\substack{j=1\\j \neq k}}^K a_j d_j(i) \widetilde{\mathbf{c}}_{jk} + \mathbf{c}_{k,L}^T \mathbf{n}_k(i).$$
(38)

Upon defining $\beta_j := \mathbf{c}_{k,L}^T \widetilde{\mathbf{c}}_{jk}$, then the averaged SINR at the output of the kth user's correlation receiver can be obtained as

$$\gamma_k^{(\text{MF})} = \frac{(\mathbf{R}_k(L+1))^2 a_k^2 (N_f - 1)^2}{\sum_{j=1, j \neq k}^K a_j^2 \left| \beta_j \right|^2 + \sigma^2 (N_f - 1)},$$

$$PE_k^{(\text{MF})} = 2^{1-K} \sum_{\substack{d_1 \dots d_K \in \{-1, +1\} \\ d_k = 1}} Q$$

$$\cdot \left(\frac{\mathbf{R}_k(L+1) (N_f - 1) a_k + \sum_{j=1, j \neq k}^K \beta_j a_j d_j}{\sigma \sqrt{N_f - 1}} \right),$$

$$k = 1, \dots, K,$$
(39)

4. Performance Evaluation

It is worthy to note that channel reciprocity is essential for using the prefiltering technique. Throughout the paper, we assume that channels are reciprocal between the AP and each RT; thereby, the MISO channel coefficients can be estimated by the AP by receiving sounding pulses (the sounding pulse should be made short enough to approach $\delta(t)$) from each of the RT. Therefore, the transmitter has full knowledge of (or can perfectly estimate) the MISO channel's information.

We first assume the average power of the path with index l=0 to be normalized to be unity, that is, $\Omega_0=1$. The log-normal fading amplitude ξ_l is generated by $\xi_l=\exp(\kappa_l)$, where κ_l is a Gaussian random variable, $\kappa_l\sim N(\mu_l,\sigma_l^2)$. To satisfy the second moment of the log-normal random variable [24], $E\{\xi_l^2\}=\exp(2(\mu_l+\sigma_l^2))=\Omega_0\exp(-\rho l)$, we have $\mu_l=-\sigma_l^2-(\rho l/2)$. We apply $\rho=0.1,\sigma_l^2=1$ in all simulation examples (i.e., $\kappa_l\sim N(-1-(l/20),1)$). For a fixed L, we generate 100 sets of channel parameters, $\{\alpha_{mk,l}\}_{l=0}^L$. Each data set is employed for simulation, and the result is obtained by taking average of the 100 independent trials.

Without loss of generality, we assume that user 1 is the desired user hereafter. Unless otherwise mentioned, we set the parameters $N_f=20$, $N_c=35$, L=15, P=20, K=10, and each user's SNR, which is defined as $SNR_k := 10 \log (a_k/\sigma)^2$, is set to be 15 dB throughout all the simulation examples. Figure 2 presents the averaged SINR (y_1) with respect to the number of transmitting antennas M, where the TR MF, LS (as M < K(L+P)/P), and ZF (as $M \ge K(L+P)/P$) schemes are provided for comparison. It is verified for both the ZF- and LS-based prefilters that system performance improves as M increases (larger transmit diversity), nevertheless, the performance of the TR MF scheme is only slightly improved. This may result from the increase of interference power for larger M in the TR MF scheme. Figure 3 shows both the y_1 and BER performance with respect to SNR₁, where the performance of TR MF (M = 20), TR MF (M = 10), ZF (M = 20), and LS (M = 10) are displayed for comparison. As expected,

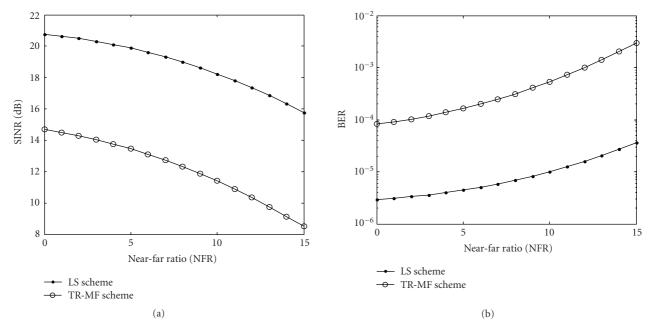
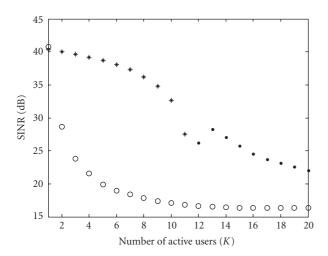


FIGURE 4: System performance with respect to near-far ratio (NFR) for the TR MF and LS schemes. (a) SINR performance with respect to the near-far ratio (b) BER performance with respect to the near-far ratio.



- * ZF scheme
- LS scheme
- O TR-MF scheme

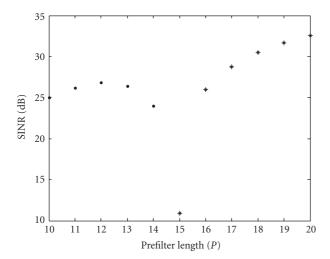
FIGURE 5: SINR performance with respect to the number of active users.

 y_1 increases (BER decreases) in accordance with SNR₁. The ZF scheme performs the best among the four curves since MUI has been completely removed. To measure the near-far resistance characteristics of the TR MF and the LS schemes (the ZF scheme is essentially near-far resistant), we first set all but one of the interferers' (e.g., the kth user) amplitudes to be the same as the desired user, $a_1 = a_2 = \cdots = a_{k-1} = a_{k+1} = \cdots = a_K$, and define the near-far ratio (NFR) as the power ratio, $(a_k/a_1)^2$ (in dB). The performance in terms of y_1 and BER with respect to NFR is depicted in Figures

4(a) and 4(b), respectively, where we set M = 10. As we vary NFR from 0 to 15 dB, y_1 slowly decays, nevertheless, it is still above 8 dB when NFR is as large as 15 dB. This demonstrates that both schemes are applicable in practical near-far environment. Figure 5 presents y_1 with respect to the number of active users, where we set M = 20. The TR MF, ZF (as $K \le MP/(L+P)$), and LS (as K > MP/(L+P)) schemes are provided for comparison. As verified by the simulation results, the proposed ZF and LS based schemes are essentially robust to MUI, whereas the performance of TR MF scheme degrades as K increases. Specifically, γ_1 of both TR MF and ZF schemes coincide at K = 1 (single user). This is due to the fact that the TR MF scheme is optimum in single-user case. In the final simulation example, we attempt to measure y_1 of the ZF and the LS schemes with respect to prefilter length, P. Let M = 20, L = 15 and K = 10, thus, LS scheme is implemented as P < KL/(M-K) = 15, and ZF-based scheme is applied when $P \geq 15$. We can verify from Figure 6 that increasing the temporal diversity effectively enhances system performance.

According to the above results, several remarks can be made.

- (1) Though ZF-based scheme outperforms TR-MF-based scheme, nevertheless, the ZF scheme is only applicable when $K(L+P) \le MP$. For example, if P = L, then the number of antenna must be at least twice as large as the number of active users $(K \le M/2)$.
- (2) It is well known that applying a ZF filter (or equivalently, decorrelating detector) in the receiver to remove MUI will enhance the additive background noise [25]. Whereas, the power normalization factor η_k dominates system performance of the ZF-based



- LS scheme
- * ZF scheme

FIGURE 6: SINR performance of the ZF and LS schemes with respect to prefilter length.

prefiltering scheme, a decrease of this leads to performance degradation. As depicted in (18), several factors determine the value of η_k , for example, as K increases, η_k decreases as well. We have verified in Figure 5 that larger K deteriorates system performance of the ZF-based prefiltering scheme.

5. Conclusions

Prefiltering-based multiuser interference suppression techniques have been applied in pulsed UWB system over MISO channel. The benefit of the proposed scheme is that it lessens the burden in signal processing of the RT receiver where a simplified correlation receiver is typically required. The simulation results have demonstrated that the proposed scheme can effectively mitigate near-far problem and suppress MUI. Though binary (antipodal) PAM scheme has been considered in this paper, extension to PPM scheme is without conceptual difficulty.

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