Research Article

An Entropy-Based Propagation Speed Estimation Method for Near-Field Subsurface Radar Imaging

Daniel Flores-Tapia¹ and Stephen Pistorius²

¹ Department of Medical Physics, CancerCare Manitoba, Winnipeg, MB, Canada ² Department of Physics and Astronomy, University of Manitoba, Winnipeg, MB, Canada

Correspondence should be addressed to Daniel Flores-Tapia, daniel.florestapia@cancercare.mb.ca

Received 26 June 2010; Revised 12 November 2010; Accepted 14 December 2010

Academic Editor: Douglas O'Shaughnessy

Copyright © 2010 D. Flores-Tapia and S. Pistorius. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

During the last forty years, Subsurface Radar (SR) has been used in an increasing number of noninvasive/nondestructive imaging applications, ranging from landmine detection to breast imaging. To properly assess the dimensions and locations of the targets within the scan area, SR data sets have to be reconstructed. This process usually requires the knowledge of the propagation speed in the medium, which is usually obtained by performing an offline measurement from a representative sample of the materials that form the scan region. Nevertheless, in some novel near-field SR scenarios, such as Microwave Wood Inspection (MWI) and Breast Microwave Radar (BMR), the extraction of a representative sample is not an option due to the noninvasive requirements of the application. A novel technique to determine the propagation speed of the medium based on the use of an information theory metric is proposed in this paper. The proposed method uses the Shannon entropy of the reconstructed images as the focal quality metric to generate an estimate of the propagation speed in a given scan region. The performance of the proposed algorithm was assessed using data sets collected from experimental setups that mimic the dielectric contrast found in BMI and MWI scenarios. The proposed method yielded accurate results and exhibited an execution time in the order of seconds.

1. Introduction

Subsurface Radar (SR) is a reliable technology that is currently used for an increasing number of nondestructive inspection applications [1-5]. SR techniques are used to image and detect inclusions present in a given scan region by processing the reflections produced when the area is irradiated using electromagnetic waves. Some advantages of SR technology are the use of nonionizing radiation and a highly automated and/or portable operation [1]. Targets present nonlinear signatures in raw SR data that difficult the proper determination of the correct dimensions and locations of the inclusions inside the scan region [6, 7]. This phenomenon is caused by the different signal travel times along the scan geometry and the wide beam width exhibited by antennas that operate in the Ultra Wide Band (UWB) frequency range. To properly detect and visualize the inclusion responses, SR datasets must be properly reconstructed.

Several reconstruction techniques have been proposed to form SR images [2, 5–8]. These approaches transfer the recorded responses from the spatiotemporal domain where they were collected to the spatial domain where the data will be displayed. Since SR image formation methods use either the time of arrival of the recorded responses or the wavenumber of the radiated waveforms, the wave speed in the propagation medium is required to accurately map the target reflections to their original spatial locations. This value can be obtained from offline measurements using a representative sample of the materials forming the scan area or by using an estimation technique. Any errors in the estimate will cause shifts in the location of the reconstructed responses and the formation of artifacts.

To determine the propagation speed in SR scenarios, a wide variety of estimation techniques have been proposed. These approaches can be divided into two main categories, focal quality measurement techniques and wave modeling approaches. Focal quality measurement techniques reconstruct the collected datasets using different propagation speed values and calculate a focal quality metric that is used to determine a suitable estimate [9–11]. Wave modeling, also called tomographic, techniques perform a minimization process by solving iteratively Maxwell's equations for a set of possible scan scenarios until the difference between the measured data and the analytical solution satisfies a stop criterion [12–15]. Techniques in both categories have been validated on experimental data, yielding accurate results in far-field SR imaging settings.

In the last decade, SR has been used for a series of novel near-field imaging scenarios, such as Breast Microwave Radar (BMR) and Microwave Wood Inspection (MWI). The targets in these applications have sizes in the order of millimetres making necessary the use of large bandwidth waveforms (>5 GHz) to achieve spatial resolution values within this order of magnitude. To the best of the authors' knowledge, only a few propagation speed estimation techniques for this SR imaging setting have been proposed [16–18]. Nevertheless, these methods have some limitations that can potentially limit their use in realistic scenarios. The parametric search proposed in [16] requires a large number of datasets from the scan region to generate accurate estimates. The wave modeling approaches presented in [17, 18] rely on computationally intensive procedures that result in processing times that can range from several minutes to a couple of days [17, 18], resulting in low data throughput rates. Additionally, the method proposed in [17] has limited use when the radiated waveform has a bandwidth over 3 GHz, which is quite common in BMR and MWI scenarios.

This paper proposes a novel technique to accurately determine the propagation speed in near-field SR scenarios. This technique reconstructs a given dataset using different propagation speed values and calculates the Shannon entropy to measure their focal quality. The value used to form the minimum entropy image is then processed to estimate the propagation speed in the scan region. Entropy metrics have been used for airborne radar to estimate the motion parameters of a given target and in SR to eliminate artifacts in reconstructed images arising from a random air-soil interface [19, 20]. The entropy of a radar image is an indicator of its focal quality. As the image is blurred, the uncertainty in the location and dimensions of a target increases. On the other hand, as the focal quality increases, the uncertainty in the position and size of each inclusion decreases. Therefore, the best focal quality is achieved when the entropy of the reconstructed SR image is minimized [21]. The proposed technique exhibits a number of improvements over standard propagation speed estimation methods for near-field imaging, including lower execution time and the ability to generate accurate results using a single data set. This paper is organized as follows. The signal model is described in Section 2. In Section 3 the proposed approach is explained. In Section 4, the performance of the proposed technique is assessed using experimental data sets. Finally, concluding remarks can be found in Section 5.



FIGURE 1: Simulated data set.

2. SR Imaging in Homogeneous Media

2.1. Signal Model. Consider a linear scan geometry formed by *M* scan locations in the (x, y) plane. The problem domain contains *T* targets over the intervals $[0, x_{max}]$ on the *x* axis and $[0, y_{max}]$ on the *y* axis and is assumed to have a constant propagation speed *v*. The distance between the scan location and the *p*th target is given by $D_p(x) = \sqrt{(x_p - x)^2 + (y_p)^2}$, where (x, 0) and (x_p, y_p) are the antenna and the *p*th target coordinates, respectively. In this scan geometry, the antenna element(s) face downwards.

At (x, 0), a waveform f(t) is radiated, and the reflections from the targets inside the scan region are recorded at the same scan location. The remaining scan locations are inactive during this process. This process is repeated for each scan location. The responses recorded at this scan location can be expressed by

$$s(t,x) = \sum_{p=1}^{T} \rho_p(x) f\left(t - \frac{2\sqrt{(x_p - x)^2 + (y_p)^2}}{v}\right), \quad (1)$$

where $\rho_p(x)$ is the reflectivity of the *p*th target. Now consider the responses from the *p*th target $s_p(t,x)$. The Fourier transform of $s_p(t,x)$ along the *t* direction is given by

$$S_{p}(\omega, x) = \rho_{p}(x)F(\omega)\exp\left(-j\left(2k\sqrt{\left(x_{p}-x\right)^{2}+y_{p}^{2}}\right)\right),$$
(2)

where $k = \omega/\nu$, and it is known as the wave number. Equation (2) is known as the spherical phase function of the scan geometry.

Since the targets are located at near-field distances, the differences between travel times at adjacent scan locations are not negligible. These differences lead to the formation of hyperbolic signatures, which make it difficult to properly assess the dimension and location of the targets inside the scan region [1]. To properly visualize the dimensions and locations of these inclusions, the collected data must be



FIGURE 2: (a) Reconstructed data set using $v = 1.5 v_{sim}$. (b) Image histogram.



FIGURE 3: (a) Reconstructed data set using $v = 1.2 v_{sim}$. (b) Image histogram.

reconstructed. One of the most effective image formation algorithms for near-field SR imaging is the frequencywavenumber migration algorithm [6, 8]. This technique has been used in seismic applications for more than three decades, and it is extensively used in subsurface radar imaging. This method can be summarized as follows. First the Fourier transform of $S_p(\omega, x)$ is calculated in the x direction yielding

$$S_{p}(\omega, k_{x}) = \rho_{p}(k_{x})F(\omega, k_{x})$$

$$\cdot \exp\left(-j\left(\sqrt{4k^{2} - k_{x}^{2}}\right)\left(y_{p}\right) - jk_{x}x_{p}\right).$$
(3)

In order to transfer the data contained in $S_p(\omega, k_x)$ to the rectangular frequency space (k_x, k_y) , a mapping $\sqrt{4k^2 - k_x^2} = k_y$ is performed. The resulting spectrum is given by

$$I_p(k_x, k_y) = \rho_p(k_x) F(k_x, k_y) \cdot \exp\left(-j\left(k_x x_p + k_y y_p\right)\right).$$
(4)

Finally, the reconstructed image, i(x, y), is obtained by calculating the inverse 2D fast Fourier transform of $I_p(k_x, k_y)$.

2.2. Propagation Speed Uncertainty Effects. In the majority of the SR scenarios, it is assumed that the medium propagation speed is known a priori. This consideration can have several negative effects on the reconstructed images if there is a difference between the value used in the reconstruction process and the propagation speed of the scan region. Let us denote the propagation speed estimate v_e and the scan region propagation speed v_t . Their corresponding wavenumbers are $k_e = \omega/v_e$ and $k_t = \omega/v_t$, and the wavenumber difference is given by $\gamma = k_t - k_e$. If s(t, x) is reconstructed using v_e , the mapping function would have the form

$$g(k_e, k_x) = \sqrt{4k_e^2 - k_x^2} = \sqrt{4(k_t - \gamma)^2 - k_x^2},$$
 (5)

where the value of γ will introduce a nonlinear error in the frequency mapping process. Depending on the magnitude, two cases can occur. If $\gamma > 0$, then $k_t < k_e$ and

$$g(k_e, k_x) > g(k_t, k_x) \quad \forall (k_y, k_x).$$
(6)

The resulting spectrum has a frequency shift on the k_y axis that decreases as the k_x value increases. Since $g(k_e, k_x)$ determines the k_y spatial frequency of the reconstructed data, the mapping error will produce a nonlinear displacement on the y axis. Given that the error varies along the k_x axis, the targets in the reconstructed images will have concave signatures. Alternatively, if $\gamma < 0$, then $k_t > k_e$ and

$$g(k_e, k_x) < g(k_t, k_x) \quad \forall (k_y, k_x), \tag{7}$$

then the error introduced by the mapping process would produce convex signatures in the spatial domain. Although the length of these target signatures will not be as large as they would have been had $\underline{s}(t, x)$ been left unprocessed (due to the subtraction of the k_x term in the mapping process), the target signatures still present augmented sizes and nonlinear behaviour.

In both cases, the defocusing caused by propagation speed error can be quantified by using the histogram of the reconstructed image magnitude values. Let us consider the case where $\gamma = 0$. In this case, the histogram would contain a series of components corresponding to the different ρ_p values. As the wavenumber error increases, the length of the nonlinear signatures grows as well. The defocusing caused the target responses to spread among a larger number of magnitude levels in the image. This will result in an increased number of modes in the histogram compared to the image reconstructed using v_t . Therefore, the image sharpness decreases as the magnitude of γ increases.

To illustrate this effect, a simulated data set, $s_{sim}(t, x)$, was generated using an SR simulator developed by the authors [22]. This data set contained three point scatters located at (0.1, 0.15)m, (0.35, 0.24)m, and (0.8, 0.22)m. The irradiated signal was a Stepped Frequency Continuous Wave (SFCW) with a bandwidth of 11 GHz and a center frequency of 6.5 GHz. The propagation speed in the scan region was $v_t =$ 1×10^8 m/s. The unprocessed data set is shown in Figure 1. The image obtained by reconstructing $s_{sim}(t, x)$ using v_t and its corresponding histogram is shown in Figures 2(a) and 2(b), respectively. To evaluate the effects in the image when y > 0, $s_{sim}(t, x)$ was also reconstructed using propagation speed values of $1.5v_t$ and $1.2v_t$. The resulting images are shown in Figures 3(a) and 4(a), respectively. The histograms of the reconstructed images are given in Figures 3(b) and 4(b). Notice how the target signatures exhibit a concave shape that becomes more elongated as the wavenumber error increases. The number of modes in the histogram grows as the magnitude of γ increases as well. It can also be appreciated how the location of the targets is shifted upwards as a result of the wavenumber error.

The effects on the reconstruction process when $\gamma < 0$ were analyzed by processing $s_{sim}(t, x)$ using propagation speed values of $0.5v_t$ and $0.8v_t$. The resulting images are shown in Figures 5(a) and 6(a), respectively. Their corresponding histograms are given in Figures 5(b) and 6(b). Although the signature size in these images is smaller than in the unprocessed data set, they still have a convex shape. Similarly to when $s_{sim}(t, x)$ was reconstructed using propagation speed values greater than v_t , the spread in the target signatures causes an increase in the image energy levels. This is reflected in the additional modes in Figures 4(b) and 5(b), compared to Figure 2(a).

2.3. Entropy As a Focal Quality Metric. The focal quality of the image i(x, y) depends on the value of v_e used during the reconstruction process. Therefore, in order to determine the fitness of v_e as an accurate propagation speed estimate, the focal quality of the reconstructed data can be used as a metric. An efficient way of determining the focal quality of a radar image is by calculating its entropy. This metric measures the level of uncertainty in a random variable. Let *R* be a discrete random variable with a probability density function p(r). According to Shannon's definition [23], the entropy of *R* is given by

$$H = -\sum_{R} p(r) \log(p(r)).$$
(8)

Pun [24] defined the entropy of a digital image with *W* intensity levels as

$$H = -\sum_{W} \frac{\psi_{W}}{\Psi} \log\left(\frac{\psi_{W}}{\Psi}\right),\tag{9}$$

where ψ_w are the pixels corresponding to the *w*th intensity level on the image and Ψ is the total number of pixels in the image. It can be seen in (9) that the entropy value of an image depends on the pixel intensity distribution. To illustrate the performance of entropy as a focal quality metric, $s_{sim}(t,x)$ was reconstructed using a set of one hundred different *v* values in the interval $[0.3v_{sim}, 2v_{sim}]$; see Figure 7. The plot of the different entropy values is shown in Figure 8. Note that the minimum entropy value is located at v_{sim} .

3. Methodology

3.1. Radar Imaging in a Two-Layer Scenario. Most near-field SR scenarios have a layer formed by air or a homogeneous matching material between the scan geometry and the scan region [20, 25, 26]. This can be modeled as an observation domain O composed of two regions, denoted a O_1 and O_2 , with different propagation speeds, denoted a v_1 and v_2 , respectively. Since the dielectric properties of O_1 are usually known a priori or can be calculated offline, determining v_1 is a trivial process. On the other hand, $v_2 \in [v_{\min}, v_{\max}]$, $v_2 \in [v_{\min}, v_{\max}]$, where v_{\min} and v_{\max} are the minimum and maximum propagation speed values that are physically feasible for this scan region. Using the signal model illustrated in (1), the recorded signal from a single target in this scenario would have the form

$$s_O(t,x) = \rho_p f(t-t_p), \qquad (10)$$



FIGURE 4: (a) Reconstructed data set using $\nu = 0.8 \nu_{sim}$. (b) Image histogram.



FIGURE 5: (a) Reconstructed data set using $v = 0.5 v_{sim}$. (b) Image histogram.



FIGURE 6: (a) Reconstructed data set using $v = v_{sim}$. (b) Image histogram.



FIGURE 7: Entropy values within the interval $[0.3 v_{sim}, 2 v_{sim}]$.



FIGURE 8: Dual layer scan scenario sample geometry.

where $t_p = \sum_{q=1}^{2} (d_{q,p}(x)/v_q)$ and $d_{q,p}(x)$ and v_q are the signal travel distance and propagation speed corresponding to the *q*th region, respectively. A diagram for this generic scan geometry can be seen in Figure 8.

By dividing the total travel distance by the signal travel time, the average propagation speed is given by

$$v_p(x) = \frac{D_p}{\sum_{q=1}^2 \left(d_{q,p}(x) / v_q \right)},$$
(11)

or alternatively

$$\frac{1}{v_p(x)} = \sum_{q=1}^{2} \frac{d_{q,p}(x)}{v_q D_p}.$$
 (12)

To reconstruct the recorded data using a wavefront reconstruction approach, the stationary point in the following expression must be determined:

$$\frac{\omega(x_p - x^*)}{v_p(x^*)D} + \frac{\omega(\partial(v_p(x^*))/\partial x)D}{v_p^2(x^*)} = k_x.$$
 (13)

Obtaining a closed form expression for x^* from (13) can be difficult. A feasible approach is to perform the reconstruction process using a constant propagation value estimate, v_f , for the whole scan area. In this case the best focal quality will be achieved for the v_f value that has the smallest error for all the recorded reflections in the data set, which can be expressed as

$$v_f^* = \arg \min_{v_f} \left(\sum_{m=1}^M \left(v_f - v_p (x_m)^2 \right) \right).$$
 (14)

By taking the first derivative of the right hand of (14) and equating it to zero, we obtain

$$\left. \sum_{m=1}^{M} 2\left(\nu_f - \nu_p(x_m) \right) \right|_{\nu_f = \nu_f^*} = 0.$$
(15)

By algebraically manipulating (15), we obtain

$$\sum_{m=1}^{M} v_f^* - \sum_{m=1}^{M} v_p(x_m) = 0,$$

$$M \cdot v_f^* - \sum_{m=1}^{M} v_p(x_m) = 0,$$

$$v_f^* = \frac{1}{M} \sum_{m=1}^{M} v_p(x_m),$$
(16)

which is equivalent to averaging $v_p(x_m)$ along the *x* direction. This approach can also be used to determine the v_f value in a multitarget scenario as follows:

$$v_{f}^{*} = \arg \min_{v_{f}} \left(\sum_{p=1}^{T} \sum_{m=1}^{M} \left(v_{f} - v_{p}(x_{m})^{2} \right) \right),$$

$$\sum_{p=1}^{T} \sum_{m=1}^{M} 2\left(v_{f} - v_{p}(x_{m}) \right) \bigg|_{v_{f} = v_{f}^{*}} = 0.$$
(17)

By following a similar approach to the one used in the singletarget scenario, the result is

$$v_{f}^{*} = \frac{1}{\mathrm{MT}} \sum_{p=1}^{T} \sum_{m=1}^{M} v_{p}(x_{m}),$$

$$E\{v(x)\} = v_{f}^{*},$$
(18)

which can also be written as

$$E\{\nu(x)\} = \frac{E\{D_p(x)\}}{E\{\sum_{q=1}^{2} \left(d_{q,p}(x)/\nu_q\right)\}},$$
(19)



FIGURE 9: Block diagram of the proposed method.

where

$$E\left\{\sum_{q=1}^{2} \frac{d_{q,p}(x)}{v_{q}}\right\} = \frac{\mu_{z}}{v_{1}} + \frac{E\left\{D_{p}(x)\right\} - \mu_{z}}{v_{2}},$$
 (20)

where μ_z is the average location of the reflections from the scan region surface, $s_z(t, x)$. Note that this estimate takes into account the effects of O_1 in the signal travel time.

3.2. Propagation Speed Estimation Algorithm. Based on the previous discussion, we can now formulate a propagation speed estimation method. To detect the surface responses and estimate the average location of the targets in the dataset, the datasets were processed using the approach presented by the authors in [27]. This method uses wavelet multiscale products to eliminate the noise components in the dataset and preserve the target responses. The surface responses are characterized using the method proposed in [28]. The denoised dataset will be reconstructed using a set of feasible propagation speed values, defined as

$$\Theta \triangleq \left\{ v_c \in [v_s, v_e] \mid v_c = \frac{c(v_e - v_s)}{C} + v_s, \ c = 1, 2, \dots, C \right\}.$$
(21)

The proposed estimation method can be described as follows.

- (1) Calculate the wavelet multiscale products of the range profile $s(t, x_m)$, in the recorded data. The result of this operation is denoted as $w(t, x_m)$.
- (2) Determine the range bin $z(m) = \max(w(t, x_m))$ which corresponds to the location the surface.
- (3) Obtain the denoised range profile, s_w(t, x_m), using the method proposed by the authors in [28].
- (4) Repeat for m = 1, 2, ..., M.
- (5) Reconstruct s_w(t, x_m) using the cth value in the set Θ, yielding i^w_{vc}(x, y).
- (6) Calculate the discrete probability density function of the energy levels on the reconstructed image.
- (7) Determine the entropy value of *i*^w_{vc}(*x*, *y*), *H*(*c*), using (10).
- (8) Repeat steps (6) through (8) for each element in Θ .



FIGURE 10: (a) First experimental data set. (b) Denoised data set. (c) Entropy values for the interval $[1 \times 10^8 \text{ m/s}, 3 \times 10^8 \text{ m/s}]$. (d) Dataset reconstructed using v^* .

- (9) Determine the value, v^* , in which the minimum entropy value is achieved.
- (10) Next, the image components in $i_{v^*}^w(x, y)$ are segmented and labelled. Then \widetilde{D} is estimated using the following operation:

$$\widetilde{D} = \sum_{\beta=1}^{B} \frac{D_{\beta}}{B},\tag{22}$$

where D_{β} is the range location of the β th target centroid, and the *B* is the number of segmented objects in $i_{v^*}^w(x, y)$.

(11) The area of O_1 is calculated as follows:

$$Z = \sum_{m=1}^{M} z(m).$$
 (23)

(12) Finally, by algebraically manipulating (22), the value of v_2^* can be determined using the following operation:

$$v_2^* = \frac{Z - \widetilde{D}}{\widetilde{D}\left(\left(Z/\left(v_1 \cdot \widetilde{D}\right)\right) - (1/v^*)\right)}.$$
 (24)

By using the proportion of O_1 over the extension of O, it is possible to estimate the value of v_2 by determining the propagation speed that yields the reconstructed image with the best focal quality. A block diagram of the proposed method is shown in Figure 9.

3.3. Refraction Effects and Lossy Medium Considerations. Compared to ray tracing approaches, wave front reconstruction methods only consider the phase behavior of the recorded responses to focus the collected data. As shown in [29], the refraction produced as the radiated wavefronts penetrate into O_2 will affect the spectral support band, Ω , of the target responses along the scan direction. The spectral support band in a radar system is closely related to the size of its point spread function [7]. In a single medium scenario, the support band size is given by

$$\Omega = [2k\sin(\theta(L)), 2k\sin(\theta(-L))], \qquad (25)$$

where $\theta(L) = \tan^{-1}(L/Y)$, 2*L* is the size of the antenna radiation footprint, and *Y* is the range extension of the scan region. The refraction caused by the interface between the two mediums will change the emergence angle of the wavefronts [29], affecting the beam width coverage in O_2 . By

using the approach proposed in [7] and the Huygens-Fresnel principle, the resulting spatial bandwidth is given by

$$\Omega_O = \left[2k \left(\sin(\theta(L_O)) - \sin(\phi) \right), 2k \left(\sin(\theta(-L_O)) + \sin(\phi) \right) \right],$$
(26)

where $L_O = (-D_{\text{max}} \cdot v_2/v_1) \cdot \sin(\phi)$, $Y = D_{\text{max}}$, ϕ is the antenna divergence angle, and D_{max} is the extension of O_2 . To satisfy the Nyquist-Shannon criterion along the scan trajectory, the separation between adjacent scan location must satisfy the following rule:

$$\Delta x \le \frac{\lambda_{\max} \sqrt{((D_{\max} \cdot v_2/v_1) \cdot \sin(\phi))^2 + (D_{\max})^2}}{4((D_{\max} \cdot v_2/v_1) \cdot \sin(\phi)) + 2\sin(\phi) \sqrt{((D_{\max} \cdot v_2/v_1) \cdot \sin(\phi))^2 + (D_{\max})^2}},$$
(27)

where λ_{max} is the wavelength corresponding to the maximum frequency component in f(t).

The previous analysis can also be used to be extended to deal with lossy media, by modeling the wavenumber as

$$k(\omega) = \frac{\omega\sqrt{\varepsilon_s}}{c} + j\tau_0, \qquad (28)$$

where τ_0 accounts for the attenuation in the medium. By performing the search process over a 2D search space where $\varepsilon_s \in [\varepsilon_{r\min}, \varepsilon_{r\max}]$ and $\tau_0 \in [\tau_{\min}, \tau_{\max}]$ and evaluating the focal quality of the resulting images, an estimate of the attenuation factor in O_2 can be obtained. A similar approach was used in [20] to enhance near-field GPR images.

4. Results

In order to test the proposed method, a SFCW radar system was used. The system consists of a 360B Wiltron Network Analyzer and an AEL H Horn Antenna which has a length of 19 cm. A bandwidth of 11 GHz (1–12 GHz) was used in all the experiments. The system was characterized by recording the antenna responses inside an anechoic chamber. This reference signal was subtracted from the experiment data in order to eliminate distortions introduced by the components of the system. The data acquisition setup was surrounded by absorbing material in order to reduce undesirable environment reflections. The data was reconstructed using a 3 GHz PC with 1 GB RAM.

The proposed estimation algorithm was tested using experimental data acquired from a $3 \times 1 \times 13$ m rectangular deposit filled with dry sand. The walls of this deposit were covered with electromagnetic wave absorbing material to eliminate their responses. The targets were buried within a region of 20 cms beneath the sand surface. Different distances between the antenna and the sand surface were used in each experiment to assess the effect of the air layer in the estimation method. In the first three experiments the box was filled with silica sand which has a propagation speed of $v_{\text{silica}} = 1.745 \times 10^8$ m/s [30]. The dielectric contrast

between the scan region layers in this scenario is similar to the one present in BMI and MWI [31, 32] scenarios. The propagation speeds of the materials used in the experimental setups are shown in Table 1. The v values of materials commonly found in BMI and MWI scan scenarios are summarized in Table 2. To demonstrate the robustness of the proposed approach, the search process is performed over the interval $[1 \times 10^8 \text{ m/s}, 3 \times 10^8 \text{ m/s}]$ which is significantly larger than the range of values reported in the literature for dry sand $([1.37 \times 10^8 \text{ m/s}, 2.12 \times 10^8 \text{ m/s}])$ [33]. A total of 200 equidistant values were defined in the search interval. In the experimental setup, the antenna was mounted on a horizontal rail that was 1.2 meters above the bottom of the box. The antenna motion was controlled by a stepper motor that was connected to a custom control interface controlled by a 2 GHz PC with 1 GB RAM. In all the experiments, the step size in the x direction was 1 cm. The limit of the nearfield region, *R*, on this imaging system is given by

$$\hat{R} = \frac{2L_A^2}{\lambda_{\text{max}}} = \frac{2 \cdot (0.12 \,\text{m})^2}{0.0145 \,\text{m}} = 1.98 \,\text{m},$$
 (29)

where L_A is the largest dimension of the antenna at its phase center. Since the maximum distance between the antenna and the sandbox bottom is 1.2 m, the targets in all the experiments were at near-field distances.

The first experimental data set is shown in Figure 10(a). In this experiment, two aluminum pipes with a diameter of 3 cm and two steel pieces with a length of 2 cm and a thickness of 5 mm were used. The average separation between the antenna and the sand surface was 10 cms. Figure 10(b) shows the energy of the denoised data. Note that the target signatures are easier to visualize in this image. The clutter in the image corresponds to stationary waves caused by multiple reflections between the surface and the antenna. Nevertheless, the magnitude of these responses is less than half of the magnitude of the target signatures. Figure 10(c) shows the resulting entropy values for the images formed using the values in the search interval. For this experiment, the minimum value is located at $v^* = 2.03 \times 10^8$ m/s.



FIGURE 11: (a) Second experimental data set. (b) Denoised data set. (c) Entropy values for the interval $[1 \times 10^8 \text{ m/s}, 3 \times 10^8 \text{ m/s}]$. (d) Dataset reconstructed using v^* .

TABLE 1: Propagation speed values of the materials used in the experimental setups.

Material	Propagation speed	
Air	3×10^8 m/s	
Silica sand	$1.745 imes 10^8 ext{ m/s}$	
Desert sand	$1.89 imes10^8$ m/s	

TABLE 2: Propagation speed values of materials found in BMI and MWI scan scenarios.

Material	Propagation speed		
Canola oil	1.3416×10^8 m/s		
Fatty breast tissue	$7.071 \times 10^7 - 1.732 \times 10^8 \text{ m/s}$		
Wood (Dry)	$1.895 \times 10^8 \text{ m/s}$		
Wood (10.8% moisture)	$1.603 imes 10^8 \mathrm{m/s}$		

The difference between this value and v_{silica} is caused by higher propagation speed of the air layer (3 \times 10 8 m/s). From the mathematical model of v_f described in (22), an increase in the value of v_1 will result in an increased v_f . Substituting the values of M, v_1 , and v^* in (24) yields a value of $v_2 =$ 1.5×10^8 m/s, which has a 12% error compared to v_{silica} . The reconstructed image using v^* is shown in Figure 10(d).

Figure 11(a) shows data collected from the second experimental setup. In this case, the targets were two aluminum pipes with a diameter of 1 cm and a steel plate with a length of 7 cms and a thickness of 1 cm. The average separation

between the antenna and the sand surface was 7 cm. It can be seen that the sand surface in this experiment is closer to the antenna, which according to the modeling performed in Section 3 will result in a lower composite propagation speed estimate. Figure 11(b) shows the corresponding denoised image. The entropy values for the search interval are shown in Figure 11(c). The minimum entropy value was located at 2.04×10^8 m/s, and the corresponding propagation speed estimate was 1.63×10^8 m/s. Similarly to the last dataset, the dataset was reconstructed using v^* . The resulting image is shown in Figure 12(d). Notice increased focal quality of these

_



FIGURE 12: (a) Third experimental data set. (b) Denoised data set. (c) Entropy values for the interval $[1 \times 10^8 \text{ m/s}, 3 \times 10^8 \text{ m/s}]$. (d) Dataset reconstructed using v^* .

TABLE 3: Estimation errors and execution times of the proposed method and the HT-based estimation technique for each experimental data set.

Experiment/metric	Entropy error	Entropy execution time	HT error	HT execution time
1	$-2.45 imes 10^7 \mathrm{m/s}$	13.1 sec	$3.85 imes 10^7 \text{ m/s}$	90.1 sec
2	$-1.15 imes 10^7 \mathrm{m/s}$	12.6 sec	$3.06 \times 10^7 \text{ m/s}$	89.45 sec
3	$2 \times 10^5 \text{m/s}$	13.3 sec	$3.55 \times 10^7 \text{ m/s}$	91.6 sec
4	$1 \times 10^{6} \mathrm{m/s}$	15.1 sec	$41.1 \times 10^7 \text{ m/s}$	90.78 sec

images compared to the previous dataset. These results are consistent with the simulations presented in Section 3. As the error between propagation speed the medium and the estimate decreases, the focal quality of the image improves.

The recorded data from a third experimental setup is shown in Figure 12(a). In this setup, the same targets than in the previous experiment were used. The steel plate target was moved 7 cm deeper to observe the effect on the propagation speed estimate. The average separation between the sand surface and the antenna was 7 cm. The denoised data can be seen in Figure 12(b). The entropy values for the search interval are shown in Figure 12(c). The minimum entropy value was located at 2.17×10^8 m/s, and the corresponding propagation speed estimate was 1.743×10^8 m/s. The reconstructed image using v^* is shown in Figure 12(d).

In order to test the proposed method in a different propagation medium, four targets were buried in desert sand $(v_{desert} = 1.89 \times 108 \text{ m/s})$ [34]. In this case, the targets were aluminum pipes with a diameter of 1 cm. The average distance between the antenna and the sand surface was 6 cm. The recorded data set is shown in Figure 13(a). The result of the denoising process can be seen in Figure 13(b). The search was conducted also in the interval $[1 \times 10^8 \text{ m/s}, 3 \times 10^8 \text{ m/s}]$. The calculated entropy values are displayed in Figure 13(c).



FIGURE 13: (a) Fourth experimental data set. (b) Denoised data set. (c) Entropy values for the interval $[1 \times 10^8 \text{ m/s}, 3 \times 10^8 \text{ m/s}]$. (d) Dataset reconstructed using v^* .

The location of the minimum value $(2.3 \times 10^8 \text{ m/s})$ was shifted towards the right. This is consistent with the model presented in Section 3, as the wave propagates faster in this medium than in silica sand. The estimated value of for this data set was $1.9 \times 10^8 \text{ m/s}$. The reconstructed image using v^* is shown in Figure 13(d).

The performance of the proposed technique was compared to the algorithm described in [16] which is based on the use of the Hough Transform (HT). This technique offers a good balance between execution time and estimation accuracy. The results of this comparison are shown in Table 3. The HT technique has a higher error and a larger execution time than the proposed approach.

5. Conclusions

A novel technique for propagation speed estimation in nearfield SR scenarios is presented in this paper. The proposed algorithm focuses the data using initial estimates of the propagation speed on the media followed by the calculation of the focal quality of the reconstructed images using Shannon's entropy as a metric. A clutter removal process is performed on the data in order to allow a more accurate estimation. A search process is performed on the resulting entropy measurements in order to find the propagation speed value associated with the minimum entropy value. The proposed method yielded accurate propagation speed estimates (with an error less that 13%) and has an execution time in the order of seconds. Finally, the proposed algorithm exhibits both lower execution times and estimation errors compared to current noninvasive estimation techniques based on the use of the HT.

References

- [1] D. Daniels, *Ground Penetrating Radar*, IEE Press, London, UK, 2004.
- [2] E. Pettinelli, A. Di Matteo, E. Mattei et al., "GPR response from buried pipes: measurement on field site and tomographic reconstructions," *IEEE Transactions on Geoscience and Remote Sensing*, vol. 47, no. 8, pp. 2639–2645, 2009.
- [3] X. L. Travassos, D. A. G. Vieira, N. Ida, C. Vollaire, and A. Nicolas, "Inverse algorithms for the GPR assessment of

concrete structures," *IEEE Transactions on Magnetics*, vol. 44, no. 6, pp. 994–997, 2008.

- [4] H. Frigui and P. Gader, "Detection and discrimination of land mines in ground-penetrating radar based on edge histogram descriptors and a possibilistic K-nearest neighbor classifier," *IEEE Transactions on Fuzzy Systems*, vol. 17, no. 1, pp. 185– 199, 2009.
- [5] E. C. Fear and M. A. Stuchly, "Microwave detection of breast cancer," *IEEE Transactions on Microwave Theory and Techniques*, vol. 48, no. 1, pp. 1854–1863, 2000.
- [6] A. S. Milman, "SAR imaging by w-k migration," International Journal of Remote Sensing, vol. 14, no. 10, pp. 1965–1979, 1993.
- [7] M. Soumekh, Synthetic Aperture Radar Signal Processing with MATLAB Algorithms, Wiley-Interscience, New York, NY, USA, 1999.
- [8] R. H. Stolt, "Migration by Fourier transform," *Geophysics*, vol. 43, no. 1, pp. 23–48, 1978.
- [9] F. Ahmad, M. G. Amin, and G. Mandapati, "Autofocusing of through-the-wall radar imagery under unknown wall characteristics," *IEEE Transactions on Image Processing*, vol. 16, no. 7, pp. 1785–1795, 2007.
- [10] L. Li, W. Zhang, and F. Li, "A novel autofocusing approach for real-time through-wall imaging under unknown wall characteristics," *IEEE Transactions on Geoscience and Remote Sensing*, vol. 48, no. 1, pp. 423–431, 2010.
- [11] L. Capineri, D. J. Daniels, P. Falorni, O. L. Lopera, and C. G. Windsor, "Estimation of relative permittivity of shallow soils by using the ground penetrating radar response from different buried targets," *Progress in Electromagnetics Research Letters*, vol. 2, pp. 63–71, 2008.
- [12] S. Lambot, E. C. Slob, I. van den Bosch, B. Stockbroeckx, B. Scheers, and M. Vanclooster, "Estimating soil electric properties from monostatic ground-penetrating radar signal inversion in the frequency domain," *Water Resources Research*, vol. 40, no. 4, pp. W042051–W0420512, 2004.
- [13] S. Lambot, E. C. Slob, I. van den Bosch, B. Stockbroeckx, B. Scheers, and M. Vanclooster, "GPR design and modeling for identifying the shallow subsurface dielectric properties," in *Proceedings of the 2nd International Workshop Advanced Ground Penetrating Radar*, vol. 1, pp. 130–135, Delft, The Netherlands, 2003.
- [14] F. Soldovieri, G. Prisco, and R. Persico, "A strategy for the determination of the dielectric permittivity of a lossy soil exploiting GPR surface measurements and a cooperative target," *Journal of Applied Geophysics*, vol. 67, no. 4, pp. 288– 295, 2009.
- [15] S. Lambot, E. C. Slob, I. van den Bosch, B. Stockbroeckx, and M. Vanclooster, "Modeling of ground-penetrating radar for accurate characterization of subsurface electric properties," *IEEE Transactions on Geoscience and Remote Sensing*, vol. 42, no. 11, pp. 2555–2568, 2004.
- [16] N. Milisavljevic and A. G. Yarovoy, "An effective algorithm for subsurface SAR imaging," in *Proceedings of the IEEE Antennas* and Propagation Society International Symposium, vol. 4, pp. 314–317, San Antonio, Tex, USA, June 2002.
- [17] G. G. Gentili and U. Spagnolini, "Electromagnetic inversion in monostatic ground penetrating radar: TEM horn calibration and application," *IEEE Transactions on Geoscience and Remote Sensing*, vol. 38, no. 4, pp. 1936–1946, 2000.
- [18] D. W. Winters, E. J. Bond, B. D. Van Veen, and S. C. Hagness, "Estimation of the frequency-dependent average dielectric properties of breast tissue using a time-domain

inverse scattering technique," *IEEE Transactions on Antennas and Propagation*, vol. 54, no. 11, pp. 3517–3528, 2006.

- [19] B. C. Flores, A. Martinez, and J. Hammer, "Optimization of high-resolution-radar motion compensation via entropy-like functions," in *Proceedings of the IEEE International Symposium Digest of Antennas and Propagation*, vol. 3, pp. 1906–1909, Ann Arbor, Mich, USA, July 1993.
- [20] X. Xu, E. L. Miller, and C. M. Rappaport, "Minimum entropy regularization in frequency-wavenumber migration to localize subsurface objects," *IEEE Transactions on Geoscience and Remote Sensing*, vol. 41, no. 8, pp. 1804–1812, 2003.
- [21] J. Sok-Son, G. Thomas, and B. C. Flores, *Range-Doppler Radar Imaging and Motion Compensation*, Artech House, Norwood, Mass, USA, 2001.
- [22] D. Flores-Tapia, G. Thomas, A. Sabouni, S. Noghanian, and S. Pistorius, "Breast tumor microwave simulator based on a radar signal model," in *Proceedings of the 6th IEEE International Symposium on Signal Processing and Information Technology (ISSPIT '07)*, pp. 17–22, Vancouver, Canada, 2007.
- [23] T. M. Cover and J. A. Thomas, *Elements of Information Theory*, John Wiley & Sons, New York, NY, USA, 1991.
- [24] T. Pun, "A new method for grey-level picture thresholding using the entropy of the histogram," *Signal Processing*, vol. 2, no. 3, pp. 223–237, 1980.
- [25] C. J. Leuschen and R. G. Plumb, "A matched-filter-based reverse-time migration algorithm for ground-penetrating radar data," *IEEE Transactions on Geoscience and Remote Sensing*, vol. 39, no. 5, pp. 929–936, 2001.
- [26] O. Lopera, E. C. Slob, N. Milisavljević, and S. Lambot, "Filtering soil surface and antenna effects from GPR data to enhance landmine detection," *IEEE Transactions on Geoscience* and Remote Sensing, vol. 45, no. 3, pp. 707–717, 2007.
- [27] D. Flores-Tapia, G. Thomas, and M. C. Phelan, "Clutter reduction of GPR images using multiscale products," in *Proceedings of IASTED International Conference on Antennas, Radar and Wave Propagation (ARP '04)*, vol. 1, Banff, Canada, 2004.
- [28] D. Flores-Tapia, G. Thomas, and S. Pistorius, "Skin surface removal on breast microwave imagery using wavelet multiscale products," in *Medical Imaging: Physiology, Function, and Structure from Medical Images*, vol. 6143 of *Proceedings of SPIE*, February 2006.
- [29] G. F. Margrave, "Seismic acquisition parameter considerations for a linear velocity medium," in *Proceedings of the 67th Annual International Meetings of the Society of Exporation Geophycists*, vol. 1, Dallas, Tex, USA, 1997, paper ACQ2.6.
- [30] E. Fratticcioli, M. Dionigi, and R. Sorrentino, "A new permittivity model for the microwave moisture measurement of wet sand," in *Proceedings of the 33rd European Microwave Conference*, pp. 539–542, 2003.
- [31] J. M. Sill and E. C. Fear, "Tissue sensing adaptive radar for breast cancer detection-experimental investigation of simple tumor models," *IEEE Transactions on Microwave Theory and Techniques*, vol. 53, no. 11, pp. 3312–3319, 2005.
- [32] G. Daian, A. Taube, A. Birnboim, M. Daian, and Y. Shramkov, "Modeling the dielectric properties of wood," *Wood Science and Technology*, vol. 40, no. 3, pp. 237–246, 2006.
- [33] J. L. Davis and A. P. Annan, "Ground-penetrating radar for high-resolution mapping of soil and rock stratigraphy," *Geophysical Prospecting*, vol. 37, no. 5, pp. 531–551, 1989.
- [34] C. Mätzler, "microwave permittivity of dry sand," *IEEE Transactions on Geoscience and Remote Sensing*, vol. 36, no. 1, pp. 317–319, 1998.