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## Research Article

# Distributed Cooperative Precoding with Power Control for Cellular Systems with Correlated Antennas at the Receiver

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We consider the problem of cooperative precoding working alongside an antenna power allocation algorithm in the downlink of a correlated Multiple Input and Multiple Output (MIMO) interference channel. An analytical model for the multicell, multiuser system with receiver-side correlation is analyzed for a realistic system configuration having two antennas each at the basestation and user terminal. Based on the precoder choices of the different terminals and the per-antenna power levels requested, a criterion is proposed for maximizing the received SINR of a severely interference-limited cell-boundary user, while controlling the loss in performance of high-SINR in-cell users in the system. A distributed protocol for cooperation amongst the base stations is also proposed. System performance gains measured in terms of mean and cell-edge spectral efficiency values are provided using numerical simulations. An improvement of about 28% to the mean spectral efficiency and 115% to the cell-edge spectral efficiency is reported over single-cell beamforming. We also demonstrate that terminals with high receive-side correlation form a specific use case of this algorithm. With two antennas at the receiver and 0.9 correlation factor, an improvement of 37% in the mean spectral efficiency is reported. The proposed technique takes into account practical constraints such as limiting to a modest level the information exchanged from the user equipments to the serving base station and amongst the base stations.

### 1. Introduction

The performance of a cellular communication system operating in a spectrum reuse-one mode is severely limited by intercell interference (ICI). With aggressive spectrum reuse, the user equipments (UEs) close to cell boundaries will experience a low value for signal-to-interference-and-noise ratio (SINR), when compared with the in-cell UEs which experience a relatively high SINR value. For systems with guaranteed quality-of-service (QoS) requirements, these low SINR UEs end up limiting the overall capacity of the cell. Emerging cellular communication systems should adopt effective means to manage interference, thereby providing higher mean spectral efficiency and cell edge throughput.

The high spectral efficiency gains possible by employing multiple antennas [1, 2] at the transmitter and receiver vanish for the interference-limited cell-boundary UEs. The presence of strong antenna correlation, especially at the receiver due to UE size limitations, restricts, the gains

further. While it might be possible to beamform a single data stream to a user using multiple transmit antennas, spatial multiplexing gains are not realizable due to the rank-deficient behavior of the channel matrix. However, the transmit antenna array can be used by a strongly interfering basestation (BS) to cooperate with its neighboring BS, and strike a balance between the performance of its own UE and the neighbor's cell-boundary UE served on the same spectral resource, by selecting a precoder which minimizes interference to the latter. Partial knowledge of relative channel strengths from different antennas also helps in improving SINR either by water filling or inverse water filling, especially for correlated antenna systems. In this paper, we propose a scheme based on cooperative precoder selection with power control (CPS-PC) for interference management in reuseone cellular networks with high receive-side correlation. We also propose a distributed causal algorithm for coordinating base station transmissions and increasing the net system throughput.

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We study the benefits of CPS-PC on the downlink of a cellular network with correlated receive antennas, and make a few key contributions. First, a criterion to quantify the performance improvement for cell boundary UEs, while controlling the loss in performance of cochannel in-cell UEs, is developed based on received SINR. Second, the benefits of power sharing across antennas based on minimal feedback about the link characteristics is illustrated by taking the case of a BS with two transmit antennas. Third, a simple and effective CPS-PC scheme is proposed alongside a user grouping framework, which ensures that a cell-boundary UE in one cell shares spectral resources only with in-cell UEs in neighboring cells, and which makes the algorithm for precoder selection causal. A distributed algorithm for cooperation among BSs with per-antenna power control, which allows cochannel BSs to minimize their contribution of interference to the cell-boundary UEs is given. Finally, simulation-based performance evaluation of the proposed scheme in terms of cell-edge (5% point in the CDF) and average spectral efficiency is provided using a multicell simulator, for a system with two antennas each at the BS and UE, respectively, following the methodologies in the 3GPP LTE standard [3].

The paper is divided into sections discussing prior art, system model description, antenna power sharing framework, the proposed CPS-PC scheme, simulation results and conclusions. Throughout the paper, lower-case letters are used for scalars, boldface lower-case letters for vectors, and boldface upper-case letters for matrices. The ith element of the vector  $\mathbf{a}$  is denoted by  $\mathbf{a}^{(i)}$ , the ith column of matrix  $\mathbf{A}$  is denoted by  $\mathbf{a}^{(ji)}$  and the ith element of the set  $\mathcal{A}$  is denoted by  $\mathbf{a}^{\{i\}}$ .

### 2. Prior Art

We begin with a brief overview of some of the interference management techniques [4, 5]. A simple coordinated means for interference management is spectrum reuse which can be, for example, 1:1 (reuse in every cell) or 1:3 (reuse in every third cell). Here the cell capacity is traded to improve the throughput of low-SINR UEs. An enhancement to this approach is fractional frequency reuse (FFR) [4], where the reuse can be between 1:1 and 1:3. Advanced MIMO techniques and wideband communication schemes allow for techniques to handle interference without sacrificing effective spectrum utilization. This makes FFR a less preferred choice.

Interference management schemes such as interference avoidance and iterative water filling, which treat interference as noise, and where each transmitter acts selfishly to align its transmissions along those directions where its desired receiver experiences the least interference [6–8], are well known. Interference management can also be studied as a vector signal processing problem, where the interfering BSs based on global channel knowledge can coordinate their transmissions such that the interfering signals get aligned and appear as if they are originating from a single source [9–12]. This enables interference cancelation with appropriate

receiver algorithms. In general, the feasibility of interference alignment over a limited number of signaling dimensions is still an open problem.

The multiple antennas employed in a MIMO system increase the available degrees of freedom, which can be used for interference suppression [13, 14]. Cooperative MIMO techniques involving coordinated transmissions by adjacent cell-site BS antennas is seen as a promising approach for improving the SINR of cell-boundary users. Capacity analyses, under different sets of assumptions [15-19], show promise. In one framework, where all the BS transmission points are connected to a central processing unit (centralized multiuser MIMO precoding), and can perform coherent transmission based on channel state information (CSI) and the user data, interference can be almost fully eliminated [17-21]. However, considering the complexity involved and the large-scale coordination that needs to happen across the network, this looks as a distant reality. This will necessitate a fundamental change in the way base stations are implemented.

Since each BS can be viewed as trying to maximize the utility to the UE it is serving, this problem can also be characterized using Game Theory [22-30]. Early studies on SIR balancing using convex and nonconvex optimization methods are available in [22-24]. From a game-theoretic perspective, interference avoidance and iterative water-filling algorithms lead to a stable operating point termed as the Nash equilibrium. However, these points often turn out to be suboptimal from a network perspective and indicate inefficiency in wireless network operation [26, 27]. A solution consisting of a linear combination of beamforming vectors and zero-forcing vectors for a MISO interference channel is given in [28]. However, this solution is feasible only when the number of significantly interfered users is less than the number of transmit antennas, thereby making this solution infeasible. Moreover, some of these techniques are not applicable when a mix of single and multiple data stream users are present in the system.

# 3. System Model and Precoding Weight Computation

We consider the downlink of an OFDMA-based cellular network having K cell sites (as in Figure 1, showing 9 cell sites). Every UE<sub>k</sub> employs  $N_k$  antennas and each BS<sub>k</sub> employs  $M_k$  antennas. Each BS serves its active UEs using orthogonal time-frequency resources, and every BS reuses all the resources. Since OFDM modulation transforms the frequency selective channel into multiple flat fading channels, we assume in our analysis that the signal in each resource undergoes a flat-fading channel over its bandwidth. A more realistic frequency selectiveness within a resource is introduced in the simulations by employing an appropriate channel model. The (b, a)th channel coefficients for the links  $\mathbf{H}_{kj}$   $(N_k \times M_j)$  between  $BS_j$  and  $UE_k$  at any given instant are given by  $h_{kj}^{(ba)} = z_{kj}^{(ba)} \sqrt{cr^{-p} 10^{S/10}}$ . Here r denotes the link distance between the transmit and receive antenna arrays, p the path loss exponent and c is the median (over shadow

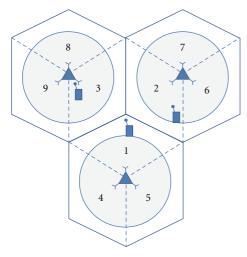


FIGURE 1: Cellular system showing in-cell and cell-edge users in an interference channel setup.

fading) of the multipath-averaged path gain at a reference distance  $(r = r_0)$ .  $S \sim \mathcal{N}(0, \sigma_S^2)$ , making  $10^{S/10}$  a log-normal shadow fading random variable, and  $z_{kj}^{(ba)} \sim \mathcal{C}\mathcal{N}(0, 1)$  represents multipath fading. The random variables  $z_{kj}^{(ba)}$  will be uncorrelated in the absence of transmit and receive array correlation. Since a system with two antennas at the BS and at the UE is widely considered as a practical configuration, we limit our discussions to this use case.

The antennas at the receiver are highly correlated due to the presence of correlated scatterers near the terminal, due to their proximity and due to UE size limitations. Correlation amongst antenna elements can be mathematically modeled using a rotation matrix R [31]. For a system with two receive antennas, this is given by  $\begin{pmatrix} 1 & \rho \\ \rho^* & 1 \end{pmatrix}$ , where  $\rho$  characterizes the degree of correlation between the array elements. The equivalent channel matrix can now be given as  $G_{kj} = R H_{kj}$ . Correlation destroys the richness of the channel, which can be characterized typically using the degree of correlation, captured by the parameter  $\kappa = \lambda_{\text{max}}/\lambda_{\text{min}}$ , defined as the ratio of the largest to the smallest eigenvalues of G. Figure 2 compares  $\kappa$  for the 2 × 2 correlated MIMO channel **G**, for  $\rho$  ranging between 0 and 1. It can be seen that the value of  $\kappa$  starts shooting up as the value of  $\rho$  exceeds 0.7. This condition happens when  $\lambda_{\min}$  starts approaching zero. Eventually as  $\rho$  approaches 1, the MIMO system starts behaving like a typical MISO system. In our work, we assume strong receive-side correlation with  $\rho = 0.9$ .

Now the matched-filtered, symbol-sampled, complex baseband data received by  $UE_k$  on the given resource for a single channel use can be given as

$$\mathbf{y}_k = \mathbf{G}_{kk}\mathbf{v}_k s_k + \sum_{j \in \delta_k} \mathbf{G}_{kj}\mathbf{v}_j s_j + \mathbf{e}_k, \quad \forall k \in \mathcal{K},$$
 (1)

where  $\mathcal{K} \triangleq \{1, 2, ..., K\}$  is the index set of the K users scheduled to use the same time-frequency resource at the different cell sites. Here  $\mathbf{y}_k$  (size  $N_k \times 1$ ) is the received signal vector and  $\mathbf{v}_k$  ( $M_k \times 1$ ) the preprocessing vector. The BSs each

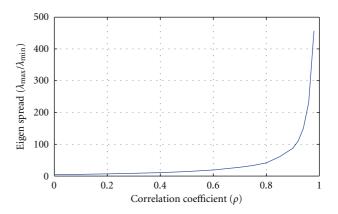


FIGURE 2: CDF of Spectral Efficiency when Basestations employ two antennas each.

transmit on a common resource a single stream of forwarderror-correction-(FEC-) coded blocks  $s_k$  to the respective UEs, chosen from a PSK or QAM alphabet set, employing multiple antennas for beamforming. The vector  $\mathbf{e}_k$  ( $N_k \times 1$ ) corresponds to the background noise at UE<sub>k</sub> of variance  $\sigma^2$ , modeled as a circularly symmetric additive white Gaussian random variable. The background noise is a superposition of the residual interference in the system and thermal noise. The transmit power at BS<sub>k</sub> is given by  $E[\|\mathbf{x}_k\|^2] = P_k$ . We assume normalized unity transmit power  $(P_k = 1)$  and make use of precoders of the form  $\mathbf{v}_k^{\dagger}\mathbf{v}_k = 1$ . This type of precoding, often termed as unitary precoding, is known to be more robust to channel quantization and variations [32].  $\mathcal{S}_k$  is the index set of the dominant interferers to  $UE_k$ . With newgeneration network deployment tools such as cell planning, antenna mast height and radiated power optimization, sectored antennas, horizontal and vertical antenna tilts, and a homogenous propagation environment, it can be ensured that the base stations neighboring a given sector will with high probability be the ones causing most of the interference to it [33]. In this work, we assume that indeed this is the case, and refer to these interferers as dominant, meaning, their removal from the system results in the UE's performance appearing to be only noise-limited (which includes residual interference). Based on system simulation studies performed along the lines of [33], the value for  $|\mathcal{S}_k|$  is typically 0 for an in-cell UE, and 1 (at sector edges) or 2 (at the cell edges), and rarely 3 or more (due to nonhomogenous propagation conditions). It is assumed that the channel parameters  $G_{kj}$  in (1) can be estimated well for all dominant interferers from their respective reference signals (pilots). In this work  $|\mathcal{S}_k|$  is assumed to be a predetermined value. If, for example,  $|\mathcal{S}_k|$  is assumed to be 2 for all UEs, then strongest two interfering BSs for each UE are modeled using channel parameters, while the remaining interferers are clubbed with the thermal noise and modeled as a Gaussian. It is assumed that the channel parameters can be estimated for these two interferers in all cases.

3.1. Performance Measure. The equalized output of the receiver is given by  $\hat{\mathbf{s}}_k = \mathbf{w}_k^{\dagger} \mathbf{y}_k$ , where  $\mathbf{w}_k$  is a  $N_k \times 1$  vector.

The effective SINR  $(\gamma_k)$  is the key parameter for designing the beamforming precoders, since the rate  $(R_k = \log(1 + \gamma_k))$  and BER can be expressed in terms of it. For a given set of precoders V,  $\gamma_k$  experienced by UE<sub>k</sub> with a maximal ratio combiner (MRC) at the receiver is given as,

$$\gamma_k = \frac{\|\mathbf{G}_{kk}\mathbf{v}_k\|^2}{\sum_{j \in \mathcal{S}_k} \|\mathbf{G}_{kj}\mathbf{v}_j\|^2 + \sigma^2}.$$
 (2)

The Effective SINR Is Given by the Ratio of the Signal Power to the Sum of the Interference Powers Leaked into  $UE_k$  and the Residual Noise. It is evident that the SINR after equalization is only a function of the signals  $(\mathbf{G}_{kj}\mathbf{v}_j)$  leaked from the different BSs. Note that  $UE_k$  can estimate  $\mathbf{G}_{kj}\mathbf{v}_j$  through training sequences. From (2), we observe that  $y_k$  of  $UE_k$  depends not only on its own beamforming vector  $\mathbf{v}_k$ , but also on the beamforming vectors of all other cochannel  $UE_j$ 's  $(\mathbf{v}_j, j \neq k)$ . This makes individual optimization of every  $y_k$  quite difficult.

High-SINR User. With conventional single-cell beamforming,  $\mathbf{v}_j$  is chosen as a function of the link  $\mathbf{G}_{jj}$  seen between  $\mathrm{BS}_j$  and  $\mathrm{UE}_j$ , to maximize the desired signal strength. Assuming a codebook  $\mathcal{V} = \{\mathbf{V}_1, \mathbf{V}_2, \ldots, \mathbf{V}_{|\mathcal{V}|}\}$  consisting of  $|\mathcal{V}|$  code vectors, we define for  $\mathbf{v}^{\{a\}} \in \mathcal{V}$ ,  $\mathcal{L}_{kj}(\mathbf{v}^{\{a\}}) = \|\mathbf{G}_{kj}\mathbf{v}^{\{a\}}\|^2$ , as the signal strength leaked from  $\mathrm{BS}_j$  into  $\mathrm{UE}_k$ . When the objective at the transmitter is to maximize signal strength at the receiver, then  $\mathrm{BS}_j$  chooses  $\mathbf{v}_j = \mathbf{v}^{\{a\}}$  which maximizes  $\|\mathbf{G}_{jj}\mathbf{v}_j\|^2$ . This increases the numerator of (2). It may be noted that this is a good choice for a in-cell user, as in this case residual interference dominates (i.e.,  $\sum_{l \in \mathcal{S}_j} \|\mathbf{G}_{jl}\mathbf{v}_l\|^2 \leq \sigma^2$ ). This is also the optimal choice in the absence of any cooperation among the different BSs.

Low-SINR User. For a user at the cell boundary intercell interference is far above the residual interference in the system (i.e.,  $\sum_{j \in \mathcal{S}_k} \|\mathbf{G}_{kj} \mathbf{v}_j\|^2 > \sigma^2$ ). This is a situation where cooperation among the different base stations will help. If the only objective of BS<sub>j</sub>,  $j \in \mathcal{S}_k$ , is to minimize the interference caused to UE<sub>k</sub>, then BS<sub>j</sub> would choose  $\mathbf{v}_j = \mathbf{v}^{\{a\}}$  which minimizes  $\|\mathbf{G}_{kj}\mathbf{v}_j\|^2$ . However, this can be deleterious for its own user  $UE_j$ . A preferred choice for  $\mathbf{v}_j = \mathbf{v}^{\{a\}}$  is one which will minimize interference at  $UE_k$  while still ensuring acceptable performance for UE<sub>j</sub>. With cooperation, BS<sub>j</sub>,  $j \in$  $\delta_k$ , chooses a compromise precoder  $\mathbf{v}_i$ , thereby reducing the value in the denominator of (2) to the extent it can afford, without sacrificing the performance of its own in-cell UE.  $BS_k$  selects  $\mathbf{v}_k$  to maximize the value in the numerator. An algorithm for such precoder-based cooperation is explained in Section 4.

Observation 1. When the user data and CSI are available at a central processing unit, as in the case of centralized multiuser MIMO precoding, it is possible to design precoders, thereby creating directional beams towards the desired user, and nulls in the direction of the interfered user. But with distributed cooperative precoding, one can only design precoders which can maximize signal strength and minimize interference leaked in the direction of the interfered user. The choice

of a codebook for closed-loop based precoding has been an extensive topic of research [34]. In the interest of simplicity, we assume the precoding vectors  $\mathbf{v}_k^{(d)}$  of the form  $\begin{bmatrix} 1 & e^{j\theta_a} \end{bmatrix}^T$ ,  $(0 \le \theta_a \le 2\pi)$  for the 2 transmit-antenna case. Such precoders change only the phase of transmission and hence are preferred due to their *constant modulus* property. Equation (1) can now be appropriately modified and rewritten for the case when  $N_r = 1$  as follows:

$$y_k = \left(g_{kk}^{(11)} + e^{j\theta_k} g_{kk}^{(12)}\right) s_k + \sum_{j \in \mathcal{S}_k} \left(g_{kj}^{(11)} + e^{j\theta_j} g_{kj}^{(12)}\right) s_j + e_k.$$
(3)

The equalized SINR  $(\gamma_{k(b)})$  of UE<sub>k</sub> can then be given as,

$$\gamma_{k(b)} = \frac{\left| g_{kk}^{(11)} + e^{j\theta_k} g_{kk}^{(12)} \right|^2}{\sum_{j \in \mathcal{S}_k} \left| g_{kj}^{(11)} + e^{j\theta_j} g_{kj}^{(12)} \right|^2 + \sigma^2}.$$
 (4)

It can be observed from (4) that the maximum value for  $y_{k(b)}$  occurs when  $\theta_k = -\frac{\left\langle g_{kk}^{(11)}g_{kk}^{(12)\dagger} \right\rangle}{\left\langle g_{kk}^{(12)\dagger}g_{kk}^{(12)\dagger} \right\rangle}$  (beamforming angle) and  $\theta_j = \pi - \frac{\left\langle g_{kj}^{(11)}g_{kj}^{(12)\dagger} \right\rangle}{\left\langle g_{kj}^{(12)\dagger}g_{kj}^{(12)\dagger} \right\rangle}$  (beam canceling angle). This condition can be approximated as closely as desired by employing a sufficiently large codebook. It may be noted that this maximum value can be obtained only when *multiuser scheduling* across cells [35] is employed. We assume that the cell-boundary UE feeds back information for its best *B* resources, in terms of data rate, each separated by at least one coherence-band (to ensure the channels are uncorrelated) and that there are *U* high-SINR users in the system, contending for scheduling in these bands. As the value of  $BU \rightarrow \infty$ , it will be possible to identify at least one resource and a corresponding in-cell UE, which has the same precoder request as the cell-boundary UE, thereby ensuring that the gain in (4) can be achieved with a probability of one.

3.2. Power Control with Cooperation. With high receive antenna correlation, gains from receive diversity, spatial multiplexing or interference rejection are not realizable. However, the multiple antennas can still be used to steer the signal power in the desired direction. In this subsection, we consider how side information about the relative channel strengths of the two transmit antennas can be used for achieving additional performance gains. Let  $\alpha^2$  and  $1 - \alpha^2$ correspond to the fixed relative power levels employed at the two antennas (keeping the total transmit power constant). We assume that  $\alpha^2 > 1/2$  without loss of generality. Feeding back information about the relative channel strengths as seen from the receiver will need one bit (e.g., indicating which among the two antennas should employ power level  $\alpha^2$ ). The effective precoding vector can thus be given as  $\left[\alpha \sqrt{1-\alpha^2}\right]^T \odot \left[1 e^{j\theta}\right]^T$ , where  $\odot$  is the element wise product operator. Equation (3) can now be appropriately modified and rewritten as follows:

$$y_{k} = \left(\alpha g_{kk}^{(11)} + \sqrt{1 - \alpha^{2}} e^{j\theta_{k}} g_{kk}^{(12)}\right) s_{k}$$

$$+ \sum_{j \in \mathcal{S}_{k}} \left(\alpha g_{kj}^{(11)} + \sqrt{1 - \alpha^{2}} e^{j\theta_{j}} g_{kj}^{(12)}\right) s_{j} + e_{k}.$$
(5)

Define  $\theta_{kj} = \theta_j - \frac{g_{kj}^{(11)}g_{kj}^{(12)\dagger}}{g_{kj}}$  as the angular offset with respect to the beamforming angle. The equalized SINR  $(\gamma_{k(p)})$  of UE<sub>k</sub> can now be given as

$$\gamma_{k(p)} = \frac{\left| \alpha \left| g_{kk}^{(11)} \right| + \sqrt{1 - \alpha^2} \cos(\theta_{kk}) \left| g_{kk}^{(12)} \right| \right|^2}{\sum_{j \in \mathcal{S}_k} \left| \alpha \left| g_{kj}^{(11)} \right| + \sqrt{1 - \alpha^2} \cos(\theta_{kj}) \left| g_{kj}^{(12)} \right| \right|^2 + \sigma^2}.$$
(6)

Let  $\phi_{\star}$  ( $\star$  used to represent either of variables i, j or k) denote the convex component (the individual terms in (6)).

$$\phi_{\star} = \left| \alpha \left| g_{k\star}^{(11)} \right| + \sqrt{1 - \alpha^2} \cos(\theta_{k\star}) \left| g_{k\star}^{(12)} \right| \right|^2$$

$$= \alpha^2 \left| g_{k\star}^{(11)} \right|^2 + (1 - \alpha^2) \left| g_{k\star}^{(12)} \right|^2$$

$$+ 2\alpha \sqrt{1 - \alpha^2} \cos(\theta_{k\star}) \left| g_{k\star}^{(11)} \right| \left| g_{k\star}^{(12)} \right|,$$
(7)

where  $|g_{k\star}^{(1a)}| \sim \text{Ray}(0,1)$ ,  $a \in \{1,2\}$  is Rayleigh distributed. When side information on the relative channel strengths across the antennas is not available at the BSs, then the only strategy possible is to transmit through each antenna with half the available power. However, when information on the relative channel strength is available, one can use it to increase the value of  $y_{k(p)}$  (by altering the individual terms of (6)).

We next evaluate the performance improvement with one bit of information about the relative channel strengths, for a fixed value of offset angle  $(\theta_{k\star})$ . Define  $h_u = \max(|g_{k\star}^{(11)}|,|g_{k\star}^{(12)}|)$  and  $h_l = \min(|g_{k\star}^{(11)}|,|g_{k\star}^{(12)}|)$ . Define  $p_{k\star} = \{+1,-1\}$  as the parameter characterizing the single power control bit. Now,  $\alpha^2$  is the power level employed on  $h_u$ . Equation (7) can now be rewritten as follows:

$$\phi_{\star} = \alpha^{2} h_{u}^{2} + (1 - \alpha^{2}) h_{l}^{2} + 2\alpha \sqrt{1 - \alpha^{2}} \cos(\theta_{k \star}) h_{u} h_{l}.$$
 (8)

Taking the mean value of (8) and then solving for  $dE[\phi_{\star}]/d\alpha=0$  gives the optimum value of  $\alpha^2$ . It can be shown that  $h_l\sim \text{Ray}(0,1/2)$  and  $h_u\sim 2$  Ray(0,1) – Ray(0,1/2). Moreover,  $h_uh_l=|g_{k\star}^{(11)}||g_{k\star}^{(12)}|$ . Substituting into (8) gives  $E[\phi_{\star}]=2\alpha^2+2\pi\cos(\vartheta_{k\star})\alpha\sqrt{1-\alpha^2}+1$ . Solving for  $dE[\phi_{\star}]/d\alpha=0$  gives  $\alpha^2=(1/2)[1\pm 1/\sqrt{1+\pi^2\cos^2(\vartheta_{k\star})}]$ . We define  $\mathcal{P}=\{(1/2)[1+1/\sqrt{1+\pi^2\cos^2(\vartheta_{kj})}],(1/2)[1-1/\sqrt{1+\pi^2\cos^2(\vartheta_{kj})}],1/2\}$  as the set of possible per-antenna power levels employable at the different BS antennas. The first two elements in the set correspond to those with one bit of power control, and the third element corresponds to the case with uniform power across the antennas. It can be seen that  $\mathbf{p}^{\{1\}}=(1/2)[1+1/\sqrt{1+\pi^2\cos^2(\vartheta_{kk})}]$  when applied to  $h_l$  helps increase the numerator value, and the same when applied to  $h_l$  helps to decrease the value in the denominator.

Figure 3 captures the array gain  $(E[\phi_{\star}])$  and array loss  $(1/E[\phi_{\star}])$  for varying offset angle. Given for comparison are three cases: without power control, with ideal power control and with one-bit power control. While the range of angles over which  $E[\phi_{\star}]$  and  $1/E[\phi_{\star}]$  is positive is 180° for the nonpower-controlled case, the same exceeds 200° with power

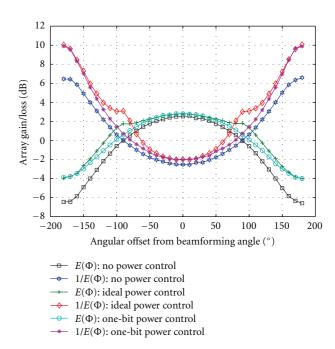


FIGURE 3: The array gain seen in a 2 Tx  $\times$ 1 Rx antenna configuration for varying offset angle with 1 – bit power control.

control. It can also be observed that power control using a single bit of information is very useful when the interfering link is made to operate as close as possible to the out-of-phase angle. Also observable is the fact that with power control, a part of the array gain lost due to the offset angle can be restored. When the interfering link is operating at the beam canceling angle, single-bit power control yields about 3 dB additional gain.

### 4. Proposed CPS-PC Algorithm

A heuristic algorithm for cooperative precoder selection with power control (CPS-PC) and multiuser scheduling, when BU is not large is explained in this section. We begin by first explaining CPS-PC without multiuser scheduling. The description of the algorithm needs an understanding of the manner in which the link behavior changes with the choice of precoder v. As per the algorithm (Algorithm 1), every  $UE_k$ computes  $\mathcal{L}_{ki}(\mathbf{v}^{\{a\}}), \mathbf{v}^{\{a\}} \in \mathcal{V}$  for the  $\mathbf{G}_{ki}$  link(s) seen from  $BS_j$ ,  $j \in \{k\} \cup \mathcal{S}_k$ , based on the reference signals (pilots) used. There is a subset of precoding vectors  $\mathcal{V}_{kj}^F$  of  $\mathcal{V}$  giving a positive value (in dB scale) for  $\mathcal{L}_{kj}$ , which we refer to as cophasing vectors, while the complementary subset  $V_{ki}^C$ which gives a negative value (in dB scale) are termed as canceling vectors. A vector  $\mathbf{l}_{kj}$  of the indices in  $\mathcal{V}$  is created by sorting the corresponding  $\mathcal{L}_{kj}(\mathbf{v}^{\{a\}}), \mathbf{v}^{\{a\}} \in \mathcal{V}$ , in decreasing order. It may be noted that  $\mathbf{v}^{\{l_{jj}^{(1)}\}}$  is the beamforming angle of BS<sub>i</sub> for UE<sub>i</sub> and  $\mathbf{v}^{\{l_{kj}^{(|\mathcal{V}|)}\}}$  the beam canceling angle of BS<sub>i</sub> for UE<sub>k</sub>. Precoding its transmission using  $\mathbf{v}^{\{\mathbf{l}_{kj}^{(|\mathcal{V}|)}\}}$  by BS<sub>i</sub> can potentially result in severe performance degradation for UE<sub>j</sub>. With cooperative precoding, however, BS<sub>j</sub>,  $j \in \mathcal{S}_k$ 

```
(1) for all i such that i \in \mathcal{K} do
  (2) UE<sub>i</sub> identifies BS<sub>i</sub>, j \in \mathcal{S}_i
          UE<sub>i</sub> estimates G_{ij}, j \in \{i\} \cup \mathcal{S}_i {link quality estimate}
          UE<sub>i</sub> computes \mathbf{l}_{ij}, j \in \{i\} \cup \mathcal{S}_i {sorted precoder index}
           UE<sub>i</sub> computes p_{ij}, j \in \{i\} \cup \mathcal{S}_i {power control choice}
           UE<sub>i</sub> forwards the p_{ij}s and l_{ij}s to BS<sub>i</sub> {feedback on-air}
  (7) end for
  (8) BS<sub>i</sub> retains \mathbf{l}_{ii}, p_{ii} and forwards \mathbf{l}_{ij}, p_{ij}, j \in \mathcal{S}_i to BS<sub>j</sub> {feedback over back-haul}
  (9) BS<sub>k</sub> serving {cell-edge}UE<sub>k</sub> chooses \mathbf{v}^{\{l_{kk}^{(1)}\}}, p_{kk} for precoding transmission to UE<sub>k</sub>
(10) BS<sub>i</sub>, j \in \mathcal{S}_k arrives at \mathbf{v}^{\{\mathbf{l}_0\}} for {precoding transmission to in-cell} UE<sub>i</sub> as follows
(11) for c = |\mathcal{V}| to |\mathcal{V}/2| do {least to minimal leakage}
           for f = 1 to |\mathcal{V}/2| do {best to minimal array gain}
(12)
               if \mathbf{l}_{ij}^{(f)} = \mathbf{l}_{kj}^{(c)} then
(13)
                    l_o \leftarrow \mathbf{l}_{ki}^{(c)} \{ \text{optimal value} \}
(14)
(15)
                    goto step (19)
(16)
                end if
            end for
(17)
(18) end for
(19) if p_{ij} = p_{kj} then
           BS_j, j \in \mathcal{S}_k employs p_o = p_{jj} \in \{\mathbf{p}^{\{1\}}, \mathbf{p}^{\{2\}}\}\ {power control employed}
(20)
(21) else
           BS<sub>j</sub>, j \in \mathcal{S}_k employs p_o = \{\mathbf{p}^{\{3\}}\} {uniform power employed}
(22)
(22) end if
```

ALGORITHM 1: The CPS-PC algorithm without multiuser scheduling.

chooses a compromise precoder  $\mathbf{v}^{\{l_o\}}$  which is in the set  $\mathcal{V}_{jj}^F \cap \mathcal{V}_{kj}^C$ . This choice of precoder can considerably minimize the interference contributed to  $UE_k$ , while restricting the loss in array gain for  $UE_j$ . In the rare case when  $\mathcal{V}_{jj}^F \cap \mathcal{V}_{kj}^C = \phi$  (empty set),  $BS_j$  picks  $\mathbf{v}^{\{l_{kj}^{(I)V/2)}\}}$ , which also exists in  $\mathcal{V}_{jj}^F$  (because  $\mathcal{V}_{jj}^F + \mathcal{V}_{jj}^C = \mathcal{V}$ ).

Similarly, when the power level requested by the cell-boundary UE is the same as the value requested by the in-cell UE  $(p_{jj} = p_{kj})$ , then BS<sub>j</sub> employs power level  $p_o$  (either  $\mathbf{p}^{\{1\}}$  or  $\mathbf{p}^{\{2\}}$ ) on the first antenna, defined by  $p_{jj}$ . When  $p_{jj} \neq p_{kj}$ , then BS<sub>j</sub> employs  $\mathbf{p}^{\{3\}}$  on both its antennas. The different UE<sub>i</sub>,  $i \in \mathcal{K}$  make the necessary measurements and then forward the quantized values  $(l_{i\star}$  and  $p_{i\star})$  to the serving BS<sub>i</sub>. The information  $(l_{ij}$  and  $p_{ij})$  needed for cooperation is then forwarded to the relevant cochannel BS<sub>j</sub>,  $j \in \mathcal{S}_i$  via the backhaul communication links. BS<sub>j</sub> then cooperates, also taking into account the feedback received from UE<sub>j</sub>.

4.1. Causality of the CPS-PC Algorithm. In a general cooperative precoding setup, the choice of precoder made by a given BS depends on the choices made by the other BSs in the cochannel set. This leads to violation of causality in precoder selection, unless the base stations employ a centralized algorithm for coordination. To overcome this problem, we employ a user grouping framework as in Figure 4, whereby adjacent cell sites do not allot the same spectral resources simultaneously to users at the cell boundaries. In this framework, the entire frequency band is divided into three (logical) subbands and the low-SINR UEs are assigned a different third of the band by neighboring cell-sites (cell-

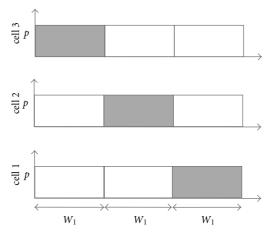


FIGURE 4: Spectrum sharing framework illustrated: the shaded part of the spectrum is used by cell edge users.

edge subband). The remaining UEs are scheduled in the remaining subbands (in-cell subband). In this framework, it is implicitly assumed that  $|\mathcal{S}_k| = 2$ . While this type of grouping is reminiscent of FFR [4], the spectral reuse here remains unity. Stated simply, this is a scheduling of UEs in the different cells, which ensures that a low-SINR UE gets interference only from BSs serving in-cell UEs on the same resource, which themselves do not require cooperation. In this setup it is the low-SINR, cell-boundary UE that requests cooperation from the interfering BSs. Each base station BS<sub>j</sub>,  $j \in \mathcal{S}_k$  serving in-cell UE<sub>j</sub> each choose a compromise precoder, based on the feedback from its own UE<sub>j</sub>, and from

TABLE 1: Gain and loss of CPS-PC.

BU	CPS gain (dB)	Avg. in-cell loss (dB)
1	1.90	0.56
2	3.65	0.27
4	4.91	0.12

UE<sub>k</sub>. In contrast, BS<sub>k</sub> employs the optimal precoding vector for beamforming to UE<sub>k</sub>. The actions of BS<sub>k</sub> are not of much consequence to UE<sub>j</sub>,  $j \in \mathcal{S}_k$ , since these are high-SINR UEs to which BS<sub>k</sub> does not generate much interference. Thus, the distributed precoder selection at all BSs is rendered causal.

4.2. CPS-PC in Practice with Multiuser Scheduling. We discussed in Section 3.1 that multiuser scheduling can mitigate the loss in performance of the in-cell UE due to cooperation asymptotically as  $BU \rightarrow \infty$ . In Section 4, we discussed Algorithm 1, which implements a compromise precoder selection without multiuser scheduling that minimizes the loss in performance for the in-cell UE. While such cooperation helps in improving the performance of the cellboundary UE, the performance of the in-cell UE would normally degrade because of the compromise precoder selected by its serving BS. However, in wide-band systems employing OFDM-based multiple access, one can employ user scheduling to make effective use of the multiuser diversity in the system and minimize the performance degradation. One simple, yet very useful, approach is for the scheduler to pair wherever possible a high-SINR UE, which happens to have the same precoder choice as the one requested by the cell-boundary  $UE_k$  of the neighboring cell. We now consider CPS-PC with multiuser scheduling and modest values for B and U, in order to overcome the loss in performance of in-cell UEs.

When multiuser scheduling is combined with the CPS-PC scheme, every BS schedules its own cell-boundary UEs in the cell-edge subbands based on the rates requested by them on each of the resource contended by them in these subbands. Typically, UEs requesting the highest rates are scheduled in those resources, which is also what we have adopted in our simulations. Once the cell-boundary UEs get scheduled, the corresponding precoder requests are shared with the interfering BSs. Based on the precoder requests received and such precoder requests from UEs associated with it, the BSs schedule the in-cell UEs on the in-cell subbands. This is done on a resource-by-resource basis. The BS tries to identify the UEs matching the same precoder requested by the cell-boundary UE, amongst those contenting for that resource. In case there is a match, the UE having the highest rate amongst them is scheduled. In the case when there is no match, the BS adds a rate offset to all those UEs contending, corresponding to a statistical measure of the offset angle given by their respective  $\mathbf{l}_{ki}$ s, and then schedules the UE with the given offset and serves with a correspondingly reduced rate. This continues, until a UE is identified to be scheduled on that resource. The probability of identifying an in-cell UE having the same

precoder request as the cell-boundary UE of an adjacent sector, or a corresponding compromise can be shown to be,

$$\Pr\left(l_{o} = l_{kj}^{\{i\}}\right)$$

$$= \begin{cases} 1 - \left(\frac{1}{2}\right)^{BU}, & \text{for } i = |\mathcal{V}|, \\ \left(1 - \left(\frac{i - |\mathcal{V}|/2}{i - |\mathcal{V}|/2 + 1}\right)^{BU}\right) \\ \times \left(\frac{i - |\mathcal{V}|/2 + 1}{|\mathcal{V}|}\right)^{BU}, & \text{for } |\mathcal{V}| > i > \frac{|\mathcal{V}|}{2}, \\ \left(\frac{1}{|\mathcal{V}|}\right)^{BU}, & \text{for } i = \frac{|\mathcal{V}|}{2}, \\ 0 & \text{else where.} \end{cases}$$
(9)

This probability is seen to be a function of the product BU. For the case when  $N_k = 1$ ,  $M_k = 2$  and  $|\mathcal{S}_k| = 2$ , for all k, the array gain and loss for some typical values of BU are given in Table 1. We can see that as BU approaches even modest values such as 4, the loss incurred by the in-cell UE becomes negligible. Similarly, the choice of the power control parameters can be shown to have the following distribution,

$$\Pr\left(p_{o} = \mathbf{p}^{\{i\}}\right)$$

$$= \begin{cases} \frac{1}{2}\left(1 - \left(\frac{1}{2}\right)^{BU}\right), & \text{for } i \in \{1, 2\} \text{ (when } p_{jj} = p_{kj}), \\ \left(\frac{1}{2}\right)^{BU}, & \text{for } i = 3 \text{ (when } p_{jj} \neq p_{kj}). \end{cases}$$

$$(10)$$

We have illustrated using system performance metrics in Section 5 that this cooperation strategy when combined with multiuser scheduling is indeed beneficial for both in-cell and cell-edge users. Note that this approach to cooperation requires knowledge of  $\mathbf{l}_{kj}$  and  $p_{kj}$  corresponding to links  $g_{ki}^{\star \star}$  of (cell-boundary) UE<sub>k</sub> at BS<sub>j</sub>. This requires a modest amount of back-haul capacity between BSs, apart from the on-air feedback from  $UE_k$  to  $BS_k$ . This type of feedback complements the link-adaptation-related feedback present in existing cellular systems. The UEs also need to know the choice made for  $\mathbf{v}^{\{l_o\}}$  in order to equalize correctly. This can be either ensured through explicit feed-forward transmission, or by transmitting precoded pilots to facilitate estimation by UE<sub>i</sub> of the combined channel  $G_{ij}v_i$ . CSI acquisition and feedback between BSs is the price to be paid in order to achieve the true gains of such cooperation strategies. Given the complexity of network deployments and the sensitivity of this feedback information to delays and errors, it is necessary that the feedback rate be kept low, but made available via low-latency links.

In summary, the CPS-PC scheme proposed in this paper, employs a simple distributed algorithm for cooperation.

With a modest amount of CSI exchange amongst adjacent cell BSs, this scheme enables the BSs to decide on a precoder that will minimize the signal strength leaked into adjacent sectors. The user grouping framework ensures that the precoder selection amongst cooperating BSs remain causal. It also ensures that interference-limited UEs benefit from a minimized interference leakage from adjacent cells. The number of dominant interferers is assumed to be two. However, this number can be extended to handle more interferers, provided the user grouping framework is appropriately modified. Multiuser diversity scheduling ensures that the choice of precoder desired by the cell-edge UE can be ensured without compromising on the link performance of a cooperating BS to its own UE. Since the proposed scheme assumes the existing network infrastructure in its design, there is no need for any framework change for adoption into emerging broadband wireless systems.

#### 5. Performance Results

In this section, we present simulation results for the proposed CPS-PC scheme. In the first part of this section, we compare, using link-level simulations, the proposed cooperation scheme with the MISO interference channel solutions in [27] and conventional single-cell beamforming. This is followed by numerical evaluation in the 3GPP LTE framework of the performance improvement possible with the proposed basestation cooperation scheme in a multicell, multiuser system, over single cell beamforming.

5.1. Link Performance Comparison. Figure 5 compares the average rate achieved, in terms of bits per-channel usage (bpcu) for varying signal-to-noise ratio (SNR), of the proposed CPS-PC scheme with the game-theory based solutions of zero-forcing and Nash equilibrium [26, 27]. Performance comparisons are made for a cell-boundary UE experiencing a signal-to-interference ratio (SIR) of 0 dB each from the cochannel transmission of two BSs, employing two antennas each. After including the thermal noise and residual interference, the effective SINR is well below  $-3 \, dB$ for this interference profile. The user grouping framework discussed in Section 4.1 is employed. The constant modulus codebook introduced in Section 3.1 were employed in the simulations. The transmit power levels are either  $\mathcal{P}_q = \{(1/2)[1 + 1/\sqrt{1 + \pi^2/2}], (1/2)[1 - 1/\sqrt{1 + \pi^2/2}]\}$  or  $\mathcal{P}_q = \{1/2, 1/2\}$ . To ensure better averaging of the results, snapshot simulations spanning 10<sup>5</sup> channel realizations were performed. The beamforming-based schemes (cooperation with and without power control) employ codebooks of size 4 and 8, respectively, whereas in the case of zero-forcing and Nash equilibrium, ideal CSI is assumed to be available at the BSs. The averaging is done over 10<sup>5</sup> channel realizations.

It can be seen from Figure 5 that the proposed cooperative precoding algorithms perform better than the gametheoretic solutions. This is due to the fact that the solutions based on game theory are inherently biased in favor of the entity with the highest bargain power (in this case, the incell UEs). At the Nash equilibrium point, the gain from

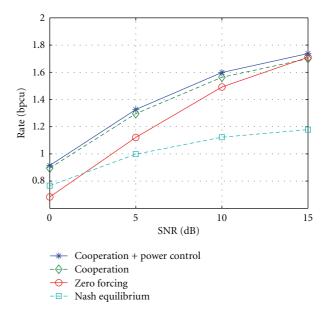


FIGURE 5: Average rates for the different transmission schemes with 2-antennas at the basestation for varying average SNRs (all channels are i.i.d. Rayleigh fading).

single-cell precoding is maximized, but nothing is done to mitigate interference. In contrast, zero-forcing by a BS helps in minimizing much of the interference created to the adjacent cell user, without any regard to the performance of the link to its own UE. In the proposed cooperation algorithm, we allow the serving BSs to beamform to the celledge UEs and the interfering BSs (serving high-SINR UEs on cochannel resources) to reduce some of the interference they cause to the cell boundary UEs. At very high SNR, the ZF performance approaches the cooperation performance. However, in terms of feedback overhead needed, both the beamforming and cooperation schemes clearly have an edge.

5.2. System Performance Evaluation. While the link simulations give a perception of how a typical cell-edge UE will perform, they do not capture the network level gains. To gain insight into this behavior we compare the gains of the proposed algorithm over the state-of-art in the 3GPP LTE framework.

5.2.1. Models and Assumptions. Some of the simulation assumptions made regarding the cellular model used are listed in Table 2, which are mostly aligned with the 3GPP framework [3]. Identical power is employed for every BS transmission and the transmit antenna array sends out signals simultaneously from all elements with 41 dBm power. The cumulative distribution function (CDF) of the SINR experienced by the users is given in Figure 6. Due to intercell interference, the SINR seen by a cell-edge user may be as low as -5 dB, compared to a value as high as 20 dB for the incell user. The OFDM system model assumed ensures that the cyclic prefix is larger than the longest delay spread in the system. The results are statistically averaged over 10<sup>4</sup> user

Table 2: Simulation parameters.

	Traffic models
User distribution	Uniform
Data generation	Full buffer
Data scheduling	Round robin with persistent allocation
	Radio network models
Distance attenuation	$L = 35.3 + 37.6 \log(d)$ , d in metres
Shadow fading	Log-normal, zero-mean with 8 dB standard deviation
Multipath fading	3GPP EPA model [36]
Cell layout	19-cell, 3 sectors/cell, hexagonal grid with wraparound
Cell radius	1000 metres intersite distance
	System models
Spectrum allocation	10 MHz bandwidth at 2 GHz
Doppler	5 Hz
Max antenna gain	15 dBi
Modulation and coding	3GPP specified [3]
Overhead	4 symbols in a subframe of 14 symbols
Feedback delay	2 msec
UE antennas	$1/2$ per UE with half-wavelength spacing, $\rho=0.9$
Network antennas	2 per site with 10-wavelength spacing
Users per cell	10, uniformly distributed

instantiations. The BSs are assumed to be interconnected via low-latency, low data-rate links.

The user grouping scheme illustrated in Figure 4 is employed. In each sector, the UEs starting from the lowest SINR are first scheduled in the one-third subband reserved for cell-boundary UEs in that sector. Once this subband is full, the remaining UEs are scheduled in the subband intended for in-cell UEs. Different UEs get serviced with different data-rates based on their instantaneous channel conditions. The different power levels employed remain the same as that in Section 5.1. The interference is modeled in the system based on the instantaneous SINR experienced by the UE. It is assumed that  $|\mathcal{S}_k| = 2$  for all UEs. In the simulations, the ideal channel parameters are assumed to be available for all the links. A BS either beamforms on the resource allocated to its cell-boundary user, or cooperates for the cochannel neighboring cell-boundary user, while simultaneously serving its in-cell user as best it can by exploiting multiuser diversity.

Since the performance improvement with basestation cooperation is dependent on the quality of CSI information estimated by the UEs and fed back to the BSs, a 5% channel estimation error, modeled as zero-mean, complex Gaussian is assumed and added to the ideal channel parameters. A single transmission per coded block, matched to the channel conditions is considered, and hybrid-ARQ is modeled as in [37]. Based on the precoder chosen, the channel realization and the active interferer set, a SINR is calculated for each link assuming a MMSE receiver model at 10% block-error rate, and then an effective SNR is calculated per downlink resource block (the time-frequency resource allocated to an user). This SNR is mapped to active radio-link data rates for each active user using the EESM prediction model [38]. In

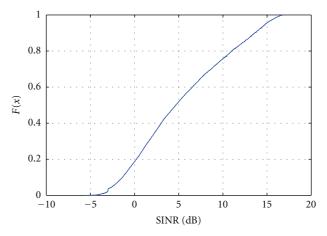


FIGURE 6: CDF of SINR experienced by a user.

practice, the network will train over the initial few subframes to arrive at the correct modulation and coding level. Since, we assume persistent scheduling for the users over tens of subframes, the prediction model can be assumed to be valid for the entire allocation. The mean and 5th percentile point of spectral efficiency are used as the metrics for average and cell-edge performance, respectively, which provide useful insight into system behavior.

5.2.2. Numerical Results. Simulation results are presented for the two cases where the UEs employ 1 and 2 antennas, respectively. We have used a codebook with four precoding vectors (i.e.,  $|\mathcal{V}| = 4$  and  $\theta_x = n(\pi/2)$ ,  $n \in \{0, ..., 3\}$ ). In conventional beamforming, the UEs feed back 2 bits to

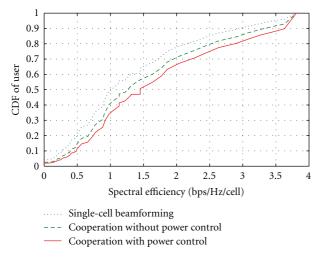


FIGURE 7: CDF of Spectral Efficiency when UEs employ one antenna each.

the serving BS for each of the B=(5) resources. There is a natural ordering of precoding vectors with respect to  $\mathcal{L}_{kj}(\mathbf{v}^{\{a\}})$ . With cooperation, the in-cell UEs feed back 2 bits for the optimal precoding vector and 1 additional bit to indicate the direction in which one should move in the naturally-ordered codebook, when the BS seeks to cooperate. With power control, one more additional bit will be employed to indicate which of the two antennas should transmit with the higher transmit power. A cell-edge UE will thus feed back 3 bits (2+1) to its serving BS and 4 bits (2+1+1) for every cooperating BS, for each of the B resources.

In Figure 7, the SE comparisons are made for the single receive-antenna case. Conventional single-cell beamforming is compared against cooperation, with and without power control. The mean SE for the three different schemes are 1.38, 1.60, and 1.77 bps/Hz/cell and the 5th percentile values are 0.13, 0.23, and 0.28 bps/Hz/cell, respectively. Cooperation helps to improve the fifth percentile point and mean spectralefficiency values by 77% and 16%, respectively. With power control, the corresponding improvement values are about 115% and 28%, respectively. There is a significant improvement in performance of the proposed cooperation scheme when power control is employed. It may be noted that the gains accrue because of both cooperation and multiuser scheduling. While cooperation ensures that the performance of the cell-boundary, low-SINR user improves, the in-cell user's performance (in the form of average throughput) does not degrade because of multiuser scheduling.

In Figure 8, the SE comparisons are made for the two-receive-antenna case. Conventional single-cell beamforming is compared against cooperation, with and without power control for a correlation coefficient  $\rho=0.9$ . To illustrate how much rate is lost because of correlation, the single-cell beamforming scheme is also compared with a value for  $\rho=0$ . In this case, the receiver can support dual-stream spatial multiplexing when in-cell, and does MMSE

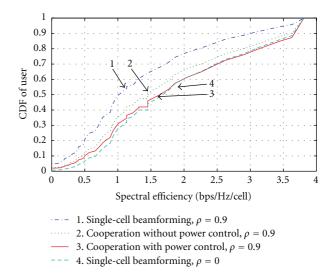


FIGURE 8: CDF of Spectral Efficiency with  $\rho=0.9$  and UEs employing two antenna each.

processing to mitigate some interference for cell-edge UEs. The mean SE of conventional beamforming for  $\rho=0$  and  $\rho=0.9$  are 1.94 and 1.40 bps/Hz/cell, respectively, and the 5th percentile values are 0.45 and 0.08 bps/Hz/cell, respectively. The correlation takes away about 28% of the mean SE gains and the 5th percentile value falls by about 82%. With  $\rho=0.9$ , mean SE value increases to 1.76 and 1.91 with and without power control, whereas the 5th percentile value increases to 0.26 and 0.32, respectively. This corresponds to a 26% and 37% improvement in the mean SE and 225% and 300% for the 5th percentile value, respectively. While the improvements seem to be very high, it may be noted that 0.32 bps/Hz/cell/user is in itself a modest value in absolute terms.

### 6. Conclusions

In this paper, we have investigated a Cooperative Precoder Selection with Power Control (CPS-PC) scheme for enhancing the performance of severely interferencelimited cell-boundary users. The problem was studied in the framework of an interference channel, the capacity of which still remains an open problem. A novel algorithm for distributed base station cooperation was proposed and the performance of this algorithm was illustrated in a practically realizable framework. A realistic system configuration with two antennas at the basestation and two at the user terminal was employed in the analysis. An analytical expression for employing power control across the transmit antennas was given. The criterion to be adopted by the different BSs when selecting the precoders while serving in-cell and cell-edge users was discussed. We demonstrated through simulations that systems with severe receive-side antenna correlation are a use case for the proposed solution. Link level analysis showed that the proposed cooperation schemes give significant gains over the game-theory based solutions of zeroforcing and Nash equilibrium. Network-level performance gains characterized in terms of the mean and 5% tail values in the spectral efficiency CDF were also provided.

The precoder-selection based algorithm for base station cooperation was shown to be useful in improving the performance of cell-edge users without compromising on the mean spectral efficiency. When employing powercontrol based cooperation, a mean spectral efficiency value improvement of about 28% is reported over conventional single-cell beamforming for a system with two transmit antennas and one receive antenna. For a system where user terminals are equipped with two receive antennas, but there is a high correlation factor 0.9 between them, a mean spectral efficiency gain of 37% is reported. It was shown that this approaches the performance of single-cell beamforming when there is no antenna correlation. The algorithm employed was shown to be simple, requiring only modest overhead when compared with single-cell MIMO signalling schemes. Furthermore, the algorithm facilitates a causal implementation of distributed precoder selection for base station cooperation. In contrast to the CPS-PC scheme, where UEs are scheduled across sectors on the same resource, in multiuser MIMO [39], UEs on the same sector with orthogonal precoder requests are scheduled on the same resource. Whereas MU-MIMO improves the cell-capacity with almost similar cell-edge performance as of single-cell beamforming, the CPS-PC scheme improves the cell-edge performance without loss in cell-capacity when compared to single-cell beamforming. Thus the two schemes employ MIMO primarily to achieve different ends.

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